THE 21-SPONGE H I ABSORPTION SURVEY. I. TECHNIQUES AND INITIAL RESULTS

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ABSTRACT

We present methods and results from "21 cm Spectral Line Observations of Neutral Gas with the EVLA" (21-SPONGE), a large survey for Galactic neutral hydrogen (H I) absorption with the Karl G. Jansky Very Large Array (VLA). With the upgraded capabilities of the VLA, we reach median rms noise in optical depth of $\sigma_r = 9 \times 10^{-4}$ per 0.42 km s⁻¹ channel for the 31 sources presented here. Upon completion, 21-SPONGE will be the largest H I absorption survey with this high sensitivity. We discuss the observations and data reduction strategies, as well as line fitting techniques. We prove that the VLA bandpass (BP) is stable enough to detect broad, shallow lines associated with warm H I, and we show that BP observations can be combined in time to reduce spectral noise. In combination with matching H I emission profiles from the Arecibo Observatory (~3!5 angular resolution), we estimate excitation (or spin) temperatures (T_s) and column densities for Gaussian components fitted to sightlines along which we detect H I absorption (30/31). We measure temperatures up to $T_s \sim 1500$ K for individual lines, showing that we can probe the thermally unstable interstellar medium (ISM) directly. However, we detect fewer of these thermally unstable components than expected from previous observational studies. We probe a wide range in column density between $\sim 10^{16}$ and $> 10^{21}$ cm⁻² for individual H I clouds. In addition, we reproduce the trend between cold gas fraction and average T_s found by the Kim et al. synthetic observations of a hydrodynamic ISM simulation. Finally, we compare methods for estimating T_s using H I observations.

Key words: ISM: clouds - ISM: structure - radio lines: ISM

1. INTRODUCTION

Star formation drives the evolution of galaxies, and the material from which stars form constantly cycles in and out of the interstellar medium (ISM). Within this process, neutral hydrogen (H I) represents a crucial transitionary stage between supernova-expelled plasma and dense star-forming gas. Consequently, the presence and influence of radiative and dynamic physical processes in the ISM are imprinted in the mass distribution of H I as a function of temperature and density. Observational constraints over the full range of temperature and density are therefore necessary for realistic heating, cooling, and feedback prescriptions within accurate models of star formation and galaxy evolution on all galactic scales (e.g., Bryan et al. 2007; Governato et al. 2010; Ostriker et al. 2010; Christensen et al. 2012; Hill et al. 2012).

Analytical models of heating and cooling in the ISM predict the existence of two neutral H I phases—the cold neutral medium (CNM) and the warm neutral medium (WNM)—each in thermal equilibrium (e.g., Pikel'ner 1968; Field et al. 1969; McKee & Ostriker 1977). McKee & Ostriker (1977) and Wolfire et al. (2003) predict that the two phases should be mostly in thermal equilibrium, with the CNM dominating and the WNM comprising only a few percent of the total H I column density. Over the range of pressures for which the two stable phases can coexist, $\sim 1000 < P/k < 8000 \text{ cm}^{-3} \text{ K}$, we theoretically expect a volume density (n) and kinetic temperature (T_k) of (n, T_K) = (5–120 cm⁻³, 40–200 K) for the CNM, and (n, T_K) = (0.03–1.3 cm⁻³, 4100–8800 K) for the WNM (Wolfire et al. 2003). Within the high-density CNM,

collisions between electrons, ions, and other H atoms can thermalize the 21 cm transition so that $T_s = T_k$. On the other hand, within the low-density WNM, collisions are not sufficient to thermalize the transition, and therefore it is widely expected that $T_s < T_k$ (e.g., Field 1958; Deguchi & Watson 1985; Liszt 2001).

In addition, the presence of H_I in the intermediate, thermally unstable regime between the CNM and WNM has a range of theoretical implications. Dynamical processes are required to maintain this unstable material, as thermal pressure alone is not sufficient to force gas across extreme density boundaries (Cox 2005). Shocks driven by supernovae into turbulent, magnetized gas create dense CNM clouds within a multiphase medium, where the fraction of thermally unstable gas is determined by the supernova rate (Koyama & Inutsuka 2002; Mac Low et al. 2005). Audit & Hennebelle (2005) showed that turbulent flow collisions produce unstable fractions of 10%-30%, depending on the amount of turbulence injected. Modeling collisions of wind-blown superbubbles, Ntormousi et al. (2011) found most gas in cold clumps, with only 8%-10% thermally unstable WNM by mass. In another colliding flow model, Clark et al. (2012) showed that the initial flow speed, including a time-dependent chemical network, has a huge effect on the resulting fractions of cold and warm gas. Clearly, observational constraints of the WNM properties and the full temperature distribution over 10–10⁴ K are important to constrain the role of self-gravity, turbulence, and large-scale gas flows in models of the ISM, as well as to guide initial conditions for numerical simulations.

1.1. Previous Work

Observationally, the hyperfine 21 cm transition of H_I provides an excellent tracer of the CNM and WNM. Given measurements of *both* H_I emission and H_I absorption, it is possible to directly measure the excitation temperature (or spin temperature, T_s) and column density (N(H_I)) of CNM and WNM structures along the line of sight (LOS). Due to the high optical depth of the CNM, 21 cm absorption signatures are easy to detect, even with low sensitivity (e.g., Lazareff 1975; Dickey et al. 1977, 1983; Crovisier et al. 1978; Payne et al. 1978; Braun & Walterbos 1992; Heiles & Troland 2003; Kanekar et al. 2003; Mohan et al. 2004; Roy et al. 2006; Begum et al. 2010). Extensive studies have been undertaken in the Milky Way, and the CNM is easily detected all the way out to a galactocentric radius of \sim 25 kpc (e.g., Dickey et al. 2009).

However, the optical depth of the WNM is so low $(\tau \leq 10^{-3})$ that extremely high sensitivity is required to detect it in absorption. Few studies have targeted individual detections of the WNM in absorption to directly measure T_s (e.g., Carilli et al. 1998; Dwarakanath et al. 2002; Murray et al. 2014), while many others estimate WNM T_s from upper limits (i.e., T_k) or as LOS averages in the presence of strongly absorbing CNM gas (Mebold et al. 1982; Heiles & Troland 2003; Kanekar et al. 2003; Kanekar et al. 2011; Roy et al. 2013a, 2013b). Therefore, the mass distribution of H I in WNM-like conditions, i.e., at high T_s and low n, is statistically unconstrained.

Previous observational studies of CNM and WNM properties, although ubiquitous, typically do not reach sufficient sensitivity to detect the WNM or thermally unstable gas directly in H_I absorption. The Millennium Arecibo 21 Centimeter Absorption-Line Survey (Heiles & Troland 2003; HT03), composed of 79 H_I absorption and emission spectral pairs spread over the full Arecibo Observatory field of view, provided important constraints on the T_s distribution of the CNM. A key result from HT03 is that 48% of the non-CNM spectral features had thermally unstable temperatures, with $500 \leqslant T_s \leqslant 5000 \text{ K}$. However, the high- T_s measurements in the HT03 study are indirect (i.e., not based on direct detections of H_I absorption). Furthermore, single-dish telescopes have the disadvantage that emission fluctuations within the beam can contaminate absorption measurements, while interferometers resolve out this large-scale structure. In addition, the HT03 results could be biased by low sensitivity. Increased integration time on non-detection sightlines from HT03 reveals absorption lines with $\tau < 10^{-3}$, as shown by Stanimirović & Heiles (2005). Previously undetected, weak absorption lines with CNM-like T_s will account for emission along the line of sight that was originally attributed to thermally unstable material, thereby reducing the estimated fraction of thermally unstable gas. Significant changes to the observed fraction of thermally unstable gas in the ISM will in turn have strong implications for the influence of any radiative and dynamic processes responsible for creating and maintaining the instability.

In a study of H I absorption at the Karl G. Jansky Very Large Array (VLA), Begum et al. (2010) demonstrated that the VLA bandpass (BP) is stable enough to detect shallow (peak $\tau \sim 10^{-3}$), wide (FWHM $\sim 7-8 \, \mathrm{km \, s^{-1}}$) absorption lines. In combination with H I emission from the Arecibo Observatory, they identified individual absorption lines with spin temperatures in the thermally unstable regime, $T_s = 400-900 \, \mathrm{K}$, in observations toward 12 bright background sources. However, only < 30% of their detected absorption lines had thermally

unstable spin temperatures, which is much lower than the 48% unstable fraction reported by HT03. This emphasized the need for a larger interferometric study of H I absorption at high sensitivity to further constrain the fractions of gas in all H I phases.

Recently, Roy et al. (2013a, 2013b) conducted an H_I absorption survey of 35 continuum sources at the Westerbork Synthesis Radio Telescope (WSRT), Giant Metrewave Radio Telescope (GMRT), and Australia Telescope Compact Array (ATCA). Using the Leiden Argentine Bonn (LAB; Kalberla et al. 2005) survey for H_I emission, they found at least 28% of the absorption-detected H_I in the thermally unstable regime (Roy et al. 2013b). However, this value is based on only 13 of their sources and the conservative assumptions that all detected CNM has $T_s = 200 \, \text{K}$ and all non-detected WNM has $T_s = 5000 \, \text{K}$, and not on direct measurements of the absorbing and emitting properties of the unstable gas.

1.2. 21-SPONGE

To measure the physical properties of all neutral H I in the ISM, we are conducting a large statistical survey, "21 cm Spectral Line Observations of Neutral Gas with the EVLA" (21-SPONGE), to obtain high-sensitivity Milky Way H I absorption spectra using the VLA. The recently upgraded capabilities of the VLA allow us to achieve median rms noise levels in optical depth of $\sigma_{\tau} = 9 \times 10^{-4}$ per 0.42 km s⁻¹ channel, which are among the most sensitive observations of H I absorption to date. Currently 31 sources are complete after over 200 hr of observing time. We have a very high detection rate so far, and we detect H I absorption in the direction of 30/31 sightlines.

In Murray et al. (2014) we applied a spectral stacking technique to the initial one-third of the 21-SPONGE sample (19 H_I absorption lines) and detected a widespread WNM component at high significance. The spin temperature of this component, equal to 7200^{+1800}_{-1200} K (68% confidence), is higher than predictions based on collisional excitation alone (<4400 K; Liszt 2001), implying that additional excitation mechanisms must be prevalent in the ISM. Ly α scattering provides a likely source for this additional excitation. However, the required density of Ly α photons necessary to explain our result is significantly higher than expectations from recent theoretical and numerical studies (e.g., Liszt 2001; Kim et al. 2014). For example, in their Galactic simulations, Kim et al. (2014) used a fixed Ly α photon number density of $10^{-6} \,\mathrm{cm}^{-3}$ and found $T_s = 4000 - 5000 \,\mathrm{K}$ for the WNM. Understanding the excitation processes of H_I, as well as the strength and topology of the Ly α radiation field, clearly requires future studies.

In Table 1, we compile properties of other single-dish and interferometric surveys for H $_{\rm I}$ absorption for comparison, including: (1) estimates of the area covered in Galactic latitude (°), (2) the angular resolution in H $_{\rm I}$ emission (arcmin), (3) the velocity resolution (km s $^{-1}$), (4) the H $_{\rm I}$ optical depth sensitivity ($\sigma_{\rm r}$) per 1 km s $^{-1}$ channels, (5) the number of H $_{\rm I}$ absorption spectra, and (6) the telescopes used for H $_{\rm I}$ absorption and emission. Those studies that targeted particular sources for measuring H $_{\rm I}$ absorption at a desired sensitivity are classified as "Absorption targeted," and those studies that mapped large spatial areas in H $_{\rm I}$ emission and then extracted absorption from continuum sources within the map are classified as "Emission mapped." We note that the four surveys

Table 1Survey Comparison

Survey	Galactic Latitude (°) (1)	Angular Res. (arcmin) (2)	Velocity Res. $(km s^{-1})$ (3)	Sensitivity $(\sigma_{r})^{a}$ (4)	Number of Spectra (5)	Telescopes (Absorption, Emission) (6)	
Absorption Targeted:	,				'		
21-SPONGE	b > 3.7	4	0.5	0.0006	58	VLA, Arecibo	
Roy et al. (2013a)	b > 1.6	36	1.0	0.0005	35	WSRT/GMRT/ATCA, LAB	
Heiles & Troland (2003)	all $ b $	4	0.16	0.002	78	Arecibo	
Stanimirović et al. (2014)	-32 < b < -8	4	0.16	0.002	27	Arecibo	
Mohan et al. (2004)	b > 15	36	3.3	0.005	102	GMRT, LDS	
Emission Mapped:		,	,	,			
VGPS ^b	b < 1.3	1	1.56	0.025-0.125	113	VLA, GBT	
CGPS ^c	-3.6 < b < 15	1	1.32	0.023-0.115	364	DRAO, DRAO 26 m	
SGPS ^d	b < 1.5	2	1.0	0.02 - 0.1	96	ATCA, Parkes	
GASKAP ^e	b < 10	0.5	1.0	0.02	>1000	ASKAP	

^a Median rms noise in H_I optical depth per 1 km s⁻¹ channel.

in the latter category were all conducted at low |b| and therefore their spectra are more complex than those at high latitude in the targeted absorption line surveys.

21-SPONGE is one of the most sensitive and extensive absorption line surveys ever undertaken. We emphasize that our analysis will improve on previous work at similar sensitivity, as we estimate physical properties of interstellar H_I using emission data obtained with spatial resolution closer to the $\sim 1''$ interferometric absorption resolution from the VLA than previous studies. For example, Roy et al. (2013a) use emission from the $\sim 36'$ wide LAB beam, and we use emission data from the Arecibo Observatory, whose beam area $(\sim 3.5 \times 3.5)$ is smaller than the LAB beam by two orders of magnitude. In addition, 21-SPONGE will occupy a unique space in terms of sensitivity and size for a long time, given that future H_I absorption surveys with the Australian Square Kilometre Array Pathfinder (ASKAP) and the Square Kilometre Array will not likely seek such high sensitivity in optical depth (e.g., McClure-Griffiths et al. 2015).

In this paper, we present the current progress of 21-SPONGE. In Section 2, we describe the observations and data reduction; in Sections 3 we discuss our methods of spectral line analysis via Gaussian fitting; in Section 4 we show example decompositions for select sources; in Section 5 we calculate temperatures and column densities for all individual component fits; in Section 6 we compare our results with previous observational surveys; in Section 7 we compare our results with synthetic observations of a hydrodynamic Galaxy simulation by Kim et al. (2014); in Section 8 we discuss the pros, cons, and biases of various methods for calculating T_s from H I emission and absorption; and in Section 9 we summarize the results.

2. DATA PROCESSING

2.1. Observations

VLA observations for 21-SPONGE began in 2011 February and targeted 58 sources from the NRAO/VLA Sky Survey

at (NVSS) catalog with flux densities 1.4 GHz $(S_{1.4 \, \text{GHz}}) > 3 \, \text{Jy}$ (Condon et al. 1998). We chose most sources to lie at high Galactic latitude ($|b| > 10^{\circ}$) to avoid complicated H_I profiles associated with the Galactic plane, and also to have angular sizes less than 1' to avoid resolving substantial continuum flux. The range of source parameters allows us to conduct observations in all array configurations and configuration moves except for D-array (most compact configuration). Currently, 53 sources have received full integration time, and 31 of these 53 have been fully reduced and analyzed. Table 2 contains information about the completed observations.

All VLA observations use simultaneously three separate, standard L-band configurations, each with one dual-polarization intermediate frequency (IF) of bandwidth 500 and 1.95 kHz per channel spacing. One IF is centered at 1.420408 GHz (H I line rest frequency, "standard"), one at 1.421908 GHz (1.5 MHz, or about 300 km s⁻¹, higher than the H_I rest frequency, called "high"), and one at 1.418908 GHz (1.5 MHz lower, called "low"). We use the high and low configurations for observing our BP calibrators to avoid contamination by local H_I in the direction of all calibrators at the H_I rest frequency. Because we normalize our solution with respect to the continuum level, the absolute phase change associated with the frequency switching method is not an issue. We use the "standard" configuration for observing target sources and measuring H_I absorption, allowing for a velocity coverage of 107.5 kms⁻¹ with 0.42 km s⁻¹ channels, corresponding to a velocity resolution of 0.5 km s⁻¹ (Rohlfs & Wilson 2004, p. 107). Relative flux calibration is performed via self-calibration on the target source, and phase and amplitude calibration are performed by observing a nearby VLA calibrator source.

For BP calibration, we observe the strong calibrators 3C286, 3C48, and 3C147 in both high and low instrument configurations following each on-source scan. For each full-length observing session (between 3 and 5 hr) we allocate up to 80% overhead for the high and low BP observations. However, if the

^b Stil et al. (2006).

^c Taylor et al. (2003).

^d McClure-Griffiths et al. (2005).

e Dickey et al. (2013).

Table 2
VLA Observation Information

Source	R.A.(J2000)	Decl. (J2000)	1	b	S _{1.4 GHz}	$\sigma_{\!\scriptscriptstyle T}$	Synthesized Beam	Time
(Name)	(hh:mm:ss)	(dd:mm:ss)	(°)	(°)	$(Jy)^a$	$(10^{-3})^{b}$	(arcsec ²)	(hr)c
4C 32.44	13:26:16	31:54:10	67.240	81.049	4.6	1.5	2.8 × 1.3	6.6
4C 25.43	13:30:37	25:09:11	22.464	80.991	6.9	0.9	2.7×1.2	2.9
3C 286	13:31:08	30:30:33	56.526	80.676	14.9	0.7	4.1×3.0	2.8
4C 12.50	13:47:33	12:17:24	347.220	70.173	5	1.3	4.2×1.5	2.8
3C 273	12:29:06	02:03:05	289.945	64.358	54.9	0.6	7.8×4.2	1
3C 298	14:19:08	06:28:35	352.159	60.667	6	0.8	2.3×1.4	2.8
4C 04.51	15:21:14	04:30:19	7.290	47.748	4	2.9	12.2×4.7	5.6
3C 237	10:08:00	07:30:16	232.117	46.627	6.5	0.9	6.5×4.4	5
3C 225A	09:42:15	13:45:51	219.866	44.025	4.4	1.5	3.9×1.6	6
3C 225B	09:42:15	13:45:49	220.010	44.007	4.4	3.0	3.9×1.6	6
3C 345	16:42:59	39:48:37	63.455	40.948	7	1.3	3.4×1.4	2.5
3C 327.1	16:04:45	01:17:51	12.181	37.006	4.1	1.4	6.1×4.8	4.7
3C 147	05:42:36	49:51:07	161.686	10.298	22.9	0.4	4.4×3.8	1.1
4C 33.48	19:24:17	33:29:29	66.388	8.373	3.8	2.8	4.8×1.8	5.7
3C 154	06:13:50	26:04:36	185.594	4.006	5.2	0.9	14×13	3.5
3C 410	20:20:06	29:42:12	69.210	-3.768	10	1.9	9.9×5.5	2.5
B 2050+36	20:52:52	36:35:35	78.858	-5.124	5	2.3	4.3×2.0	5
3C 409	20:14:27	23:34:52	63.397	-6.120	14	3.3	1.6×1.4	3.3
PKS 0531+19	05:34:44	19:27:21	186.761	-7.109	7	0.5	1.3×1.1	1.9
3C 111	04:18:21	38:01:35	161.675	-8.821	4.3	0.7	23×23	5.1
3C 133	05:02:58	25:16:24	177.725	-9.914	5.7	1.8	1.3×1.1	5.1
3C 138	05:21:09	16:38:22	187.403	-11.346	9	0.9	15×5.2	2.2
3C 123	04:37:04	29:40:13	170.581	-11.662	47	0.7	19×5.5	2.2
3C 433	21:23:44	25:04:10	74.475	-17.693	12	2.4	9.7×5.7	3
3C 120	04:33:11	05:21:15	190.373	-27.397	3.4	1.1	4.7×4.3	7
3C 48	01:37:41	33:09:35	133.961	-28.720	15.7	0.7	1.3×1.2	2.8
4C 16.09	03:18:57	16:28:32	166.633	-33.598	8	0.8	1.3×1.2	1.5
3C 454.3	22:53:57	16:08:53	86.108	-38.182	11	0.9	7.5×3.9	2.5
J 2232	22:32:36	11:43:50	77.436	-38.582	7	0.7	5.2×4.3	2.1
3C 78	03:08:26	04:06:39	174.857	-44.514	5.7	4.1	4.6×3.7	5.2
3C 459	23:16:35	04:05:17	83.038	-51.285	4	0.8	5.7×4.5	5

^a Condon et al. (1998).

source was stronger than \sim 7 Jy, it was observed as its own BP calibrator to conserve slewing time over the course of the observation, which is particularly beneficial for filler-project length observing files (maximum 1 hr total).

2.2. Data Reduction

All data sets were reduced using the Astronomical Image Processing System $^7({\rm AIPS})$. We decided to use AIPS instead of CASA 8 to take advantage of the suite of BP analysis tasks unique to AIPS when we began the survey. During observations conducted in configuration moves involving D-array, all baselines shorter than 300 m were excluded to avoid contribution from partially resolved H $_{\rm I}$ emission. After initial flagging of all observations, the task BPLOT was used to examine initial BP solutions for the high and low BP calibration observations in detail for each antenna. These solutions were then combined to produce a final BP solution. For all sources, we consistently reach noise levels in normalized BP amplitude profiles of $<10^{-3}$ per $0.42~{\rm km~s^{-1}}$ channels.

In addition to a linear slope in the BP solution, we found a stable, periodic ripple that was revealed only because of the extreme sensitivity of our observations. The ripple is caused by the finite impulse response (FIR) filters applied to the data prior to correlation and is stable in amplitude, phase, and time. The Appendix contains information on the properties and stability of the BP structure.

Furthermore, we demonstrated that the VLA BP is stable enough to combine BP observations conducted at different times or on different days. This is especially helpful for filler observations (max total observation time ≤ 1 hr). We are able to combine BP observations between separate days, thereby increasing the total BP observation time. The noise level in the BP solution decreases with added time by index of -0.44 ± 0.02 , which is nearly the theoretically expected index of -0.5 (i.e., by $1/\sqrt{t_2/t_1}$ for combined integration time t_2 and initial integration time t_1). The Appendix contains further details on the noise improvement due to time averaging in the cases of additional data sets.

Following amplitude and phase calibration on the target data set, we apply the BP solution from the combined BP calibration observation. We then perform self-calibration on the target data set by isolating the target source continuum, constructing an image, and using it to calibrate the continuum data set. After applying the self-calibration solution, we repeat the process until the signal-to-noise level in the resulting continuum image no longer improves significantly. For most sources, this occurs

^b rms noise in τ per 0.42 km s⁻¹ channel, measured off-line.

^c Total on-source time, not including calibration overheads.

http://www.aips.nrao.edu

⁸ http://casa.nrao.edu

after only two iterations. Returning to the original target data set, the continuum contribution to each source is determined by fitting a linear model to line-free channels. We subtract this from the source visibilities in all channels using the AIPS task UVLSF. We then use the task CVEL to correct source velocities for Earth's rotation and motion toward the local standard of rest (LSR) within the solar system.⁹

The final calibrated data cubes are constructed using the AIPS task IMAGR and are cleaned to three times the background noise in a test image of one channel. For each cube, the pixel sizes are calculated to be four times smaller than the beam size to properly sample the beam. Finally, we extract the absorption spectrum from the central pixel of each image, as in most cases, the sources are unresolved by the observations. However, of the 31 completed sources, 5 were resolved (3C327.1, 3C154, 3C111, 3C133, 3C123). To extract the spectra from these five data cubes, we average all spectra over the extent of the source.

The achieved sensitivities for the final data products are listed in Table 2, and the quoted values for σ_{τ} are per 0.42 km s⁻¹ channel. The median rms noise values are $\sigma_{\tau} = 9 \times 10^{-4}$ (mean 1×10^{-3}) per 0.42 km s⁻¹ channel and $\sigma_{\tau} = 6 \times 10^{-4}$ (mean 8×10^{-4}) per 1 km s⁻¹ channel. Several sources have high noise due to the fact that they were resolved by the VLA, and we plan to include additional data in these directions to reduce the noise for the final data release.

2.3. Optical Depth Comparison

To verify the accuracy of our absorption spectra, we compare integrated optical depths with two previously published surveys: the Arecibo Millennium Survey (HT03) composed of 79 absorption spectra with matching expected emission spectra from the Arecibo Observatory, and 35 high-sensitivity absorption spectra from the GMRT, WSRT, and ATCA by Roy et al. (2013a). We compare the sources overlapping between 21-SPONGE and HT03 (green diamonds) and between 21-SPONGE and Roy et al. (2013a) (black stars) in Figure 1.

The three catalogs generally agree well in terms of integrated optical depth. In Figure 1, we indicate the source names of those that differ most between the catalogs. In the cases of 4C25.43 and 3C345, Roy et al. (2013a) have better sensitivity $(\sigma_{\tau} = 5 \times 10^{-4})$ and 5×10^{-4} , whereas we achieve $\sigma_{\tau} = 13 \times 10^{-4}$ and 9×10^{-4} , respectively), so our $\int \tau(v) dv$ values have larger error bars. For source 3C273, the HT03 baseline is not perfectly flat, with the consequence that their $\int \tau(v) dv$ value is higher than ours. HT03 did not measure any H_I absorption above the 1σ limit toward 3C286, so we compare our optical depth spectrum to the higher-sensitivity result from Stanimirović & Heiles (2005; SH05) (filled green diamond) and observe that our integrated values are consistent. In addition, we agree very well with the Roy et al. (2013a) value for 3C286. Toward source 4C32.44, HT03 have lower sensitivity, and so their value has larger error bars. Finally, the HT03 profile toward 3C225A, a resolved double-lobed radio galaxy, contains "positive absorption" due to large errors in estimating H_I absorption profiles.

Remaining residual differences that exist could possibly be caused by fluctuations in absorption profiles due to transient clouds, as has been well studied in the cases of 3C147 (Lazio et al. 2009) and 3C138 (Brogan et al. 2005; Roy et al. 2012). These studies find differences in optical depth between observational epochs (spaced by several years) of up to ~0.5.

Overall, the excellent agreement between 21-SPONGE absorption and HT03, Roy et al. (2013a). and Stanimirović & Heiles (2005) absorption demonstrates that our observing and reduction strategies are sound. It is also encouraging to see that in the majority of cases, 21-SPONGE observations agree well with HT03 and Stanimirović & Heiles (2005). This proves that Arecibo—a single-dish telescope—can reliably produce accurate H $_{\rm I}$ absorption profiles in the directions of strong sources ($S_{\rm 1.4\,GHz}>3~\rm Jy$).

2.4. Matching Emission Profiles

We obtained matching H_I emission profiles along most sightlines from the 305 m Arecibo Observatory as part of project a2770. For the observations, we used the L-wide receiver to simultaneously observe H_I at 1420 MHz and three OH lines (1665, 1667, and 1720 MHz) with two linear polarizations. We achieve a velocity resolution of 0.16 km s⁻¹ over 2048 channels between -164 and 164 km s⁻¹ for the H_I observations. The ~3/5 angular resolution of the Arecibo telescope at these frequencies complements the VLA observations by minimizing the effects of mismatched beam sizes on interpreting the absorption and emission spectra. It would require prohibitively long integration times to acquire emission profiles at similar sensitivity from the VLA in D array.

Following the methods of HT03, we constructed an "expected" H $_{\rm I}$ emission profile $(T_{\rm exp}~(\nu))$ toward each source by interpolation using a pattern of 16 observed off-source positions. The expected profiles represent the profile one would observe if the continuum source were turned off. The profile construction via least-squares fit is described fully by HT03 and was also implemented by Stanimirović & Heiles (2005) and Stanimirović et al. (2014). The error in T_{exp} (v) as a function of velocity, $\sigma_{T_{exp}}(v)$, is also computed in this process based on the difference in system temperature and spatial offset between onsource and off-source pointings (HT03, Section 2.7). As discussed by Stanimirović et al. (2014), we used a simpler method than HT03 and excluded fine-tuning for gain variations under the assumption that correctly accounting for them requires accurate knowledge of the spatially varying gain and beam shape. In addition, we used a second-order Taylor expansion to construct T_{exp} (v), which, as found by Stanimirović et al. (2014), is a noisier but more accurate approach than using a first-order Taylor expansion. We then divided the expected profiles by a total beam efficiency factor of 0.85 (P. Perillat 2015, private communication) to convert the expected profiles to brightness temperature.

To compare our results, we scaled the expected emission profiles from HT03 to our new Arecibo expected emission profiles by their velocity integrals and found that applying a median beam efficiency factor of 0.81 to the HT03 profiles produced the best agreement with our beam-efficiency-scaled profiles from a2770. For each source, we then selected the scaled emission profile with the best sensitivity. For 11/31

⁹ We initially applied CVEL before continuum subtraction (UVLSF). However, we observed considerable Gibbs ringing in the edge channels of our reduced spectra. This forced us to Hanning smooth all data sets, reducing our velocity resolution by a factor of 2. After investigating the origin of the Gibbs ringing, we found that the ringing phenomenon arose in the order of CVEL and continuum subtraction, and reversing their order of application eliminated the ringing effect.

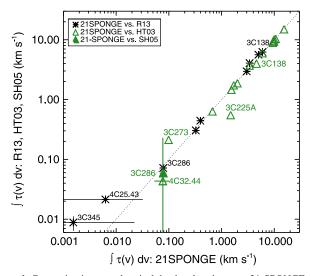


Figure 1. Comparing integrated optical depth values between 21-SPONGE and Roy et al. (2013) (R13; black stars), 21-SPONGE and HT03 (green diamonds), and 21-SPONGE and Stanimirović & Heiles (2005) (SH05; filled green diamond). The dotted line shows y=x to highlight the agreement between the majority of points. Sources that strongly deviate from y=x are indicated by their source names. Errors on the measurements are included but are smaller than the symbol sizes unless visible.

sources we use the HT03 expected emission profiles, and for 16/31 sources we use a2770 data. The remaining four sources do not have Arecibo emission profiles because they are on the edge of the Arecibo field of view, and so we use emission spectra from the LAB survey for these sources (Kalberla et al. 2005).

2.5. Stray Radiation

Due to the complex beam pattern of the Arecibo telescope, our emission profiles are likely cotaminated at some level by radiation from higher-order side lobes, known as stray radiation. To estimate the level of this contamination, we use additional data from the Galactic Arecibo L-band Feed Array Survey in H_I (GALFA-H_I; Stanimirović et al. 2006; Peek et al. 2011). GALFA-H I is an all-sky survey for H I emission in the Galaxy using the seven-beam-array ALFA receiver. Peek et al. (2011) smoothed GALFA-H I data cubes to the ~36' angular resolution of the stray radiation-corrected LAB survey (Kalberla et al. 2005) and found that the differences generally fall within typical 1σ errors (see Figure 12 in Peek et al. 2011). Stray radiation signatures appear as broad, wing-like features at high velocities, which are easy to isolate visually from the narrower, peak-like differences due to mismatched beam shapes between the LAB survey and the smoothed GALFA-H I data cubes.

To compare our results for all sources covered by GALFA-H I to date, we constructed expected GALFA-H I emission profiles around each source by averaging 5×5 pixel² regions around each source. The central pixels of this average are likely affected by absorption, so we removed the central 3×3 pixel² region, which corresponds to roughly one beam area. We then subtracted our $T_{\rm exp}$ (ν) profiles from the expected GALFA-H I profiles and found that the differences fall mostly within 3σ errors in $T_{\rm exp}$ (ν), which is very encouraging. The best method of removing the stray radiation contamination in lieu of modeling the complex, zenith-angle-dependent beam pattern of

the Arecibo telescope would be to bootstrap the GALFA-H I data to the LAB survey and simply remove the differences from our profiles (e.g., as discussed by Peek et al. 2011). However, applying this method necessarily injects noise from the LAB survey into the higher-sensitivity GALFA-H I profiles. In addition, the method assumes that the contamination to GALFA-H I (observed with ALFA) is the same as to our $T_{\rm exp}$ (ν) profiles (observed with L-wide), which may not necessarily be the case. In the future we plan to investigate alternative methods for modeling the stray radiation contribution to our emission profiles without degrading our sensitivity unnecessarily.

3. ANALYSIS

3.1. Gaussian Fitting

To estimate physical properties of individual interstellar clouds along the line of sight, we decompose the H_I spectra into Gaussian functions (e.g., HT03). Although the CNM dominates the absorption spectra, by achieving extremely high sensitivities we aim to detect shallow, wide signatures of warm gas directly in absorption.

Based on the two-phase ISM model, discussed in detail by Dickey et al. (2003) and HT03, both the CNM and WNM contribute to the expected profile, $T_{\rm exp}(\nu)$. We denote the CNM and WNM components detected in absorption by the subscript "ABS" and the WNM components detected in emission by the subscript "EM." Thus, $T_{\rm exp}(\nu)$ is given by

$$T_{\text{exp}}(v) = T_{B,\text{ABS}}(v) + T_{B,\text{EM}}(v), \tag{1}$$

where $T_{B,ABS}(v)$ is the brightness temperature due to absorption-detected gas and $T_{B,EM}(v)$ is the brightness temperature due to non-absorbing gas detected only in emission.

For each absorption spectrum, we identify a number (N) of Gaussian components using a least-squares fit (described in Section 3.3), so that the absorption spectrum $\tau(v)$ is given by

$$\tau(v) = \sum_{n=0}^{N-1} \tau_{0,n} e^{-\left[(v - v_{0,n})/\delta v_n\right]^2},$$
 (2)

where $(\tau_0, v_{0,n}, \delta v_n)$ are the (peak optical depth, central velocity, 1/e width) of the nth component in the fit.

Following the fit to the absorption spectrum, and assuming that each fit component is independent and isothermal with spin temperature $T_{s,n}$, the brightness temperature contribution from the N Gaussian functions detected in absorption to the expected emission profile is given by

$$T_{B,ABS}(v) = \sum_{n=0}^{N-1} T_{s,n} \left(1 - e^{-\tau_n(v)} \right) e^{-\sum_{m=0}^{M-1} \tau_m(v)}.$$
 (3)

Here, the subscript m and the associated optical depth $\tau_m(v)$ run through the M number of CNM clouds lying in front of cloud n.

We model the remaining contribution to the expected profile by WNM not detected in absorption using a set of Kindependent Gaussian functions. For each kth component, we assume that a fraction F_k lies in front of all N absorption components, and thus a fraction $(1 - F_k)$ is absorbed by the intervening gas. The emission brightness temperature from these K non-absorbing Gaussian components is given by

$$T_{B,EM}(v) = \sum_{k=0}^{K-1} \left[F_k + (1 - F_k) e^{-\tau(v)} \right]$$

$$\times T_{0,k} e^{-\left[(v - v_{0,k}) / \delta v_k \right]^2}, \tag{4}$$

where $(T_{0,k}, v_{0,k}, \delta v_k)$ are the (peak in units of brightness temperature, central velocity, 1/e width) of the kth emission component. For a given set of absorption components, the expected profile is fit for the spin temperatures of the Nabsorption components and the Gaussian parameters of the K emission components. This fit is repeated for all permutations of absorption components along the line of sight, for every value of F_k for each emission component. Following the method of HT03, we allow F_k to be 0, 0.5, or 1. The values of F_k affect the derivation of spin temperatures, but any finer tuning of the values produces results that are difficult to distinguish statistically. Overall, there are $N! \times 3^K$ permutations for each line of sight. The final fit selected is the one with the smallest residuals, and the final spin temperatures are calculated by a weighted average over all trials, where the weights are equal to the inverse of the variance of the residuals to the T_{exp} (v) fit (HT03). The error in the final spin temperature is estimated from the variation in T_s with F_k , as described in Section 3.5 of HT03.

The expected emission profile (Equation (1)) has been baseline-corrected, meaning that the contribution from diffuse radio continuum emission, including the cosmic microwave background (CMB) and Galactic synchrotron emission, has been removed. This value, $T_{\rm sky}$, is equal to 2.725 K from the CMB plus an estimate of the Galactic synchrotron background at the source position. Given that the spectral index of the synchrotron background is about 2.7, we divide the 408 MHz brightness temperature taken from the Haslam et al. (1982) Galactic survey by a factor of $(1420/408)^{2.7}$ to estimate the synchrotron contribution at $1420\,{\rm MHz}$. The 21-SPONGE sources are mostly at high latitude, and therefore the values of $T_{\rm sky}$ are generally small, ranging between 2.76 and 2.85 K. To account for its presence, we add $T_{\rm sky}$ back to $T_{\rm exp}$ (ν) before performing the fit.

3.2. Absorption Noise Spectra

The noise in H_I absorption spectra is not constant as a function of velocity. HI emission at Galactic velocities will increase the system temperature of the VLA antennas, producing different noise properties across the absorption spectra. To estimate the "noise spectra," $\sigma_{\tau}(v)$, of the VLA absorption profiles, we follow the methods discussed by Roy et al. (2013a). The spectral noise is composed of (1) onsource noise, $\sigma_{on}(v)$ (varies with velocity), and (2) off-line noise from the frequency-switched BP solution, σ_{BP} (constant with velocity). We first estimate the rms noise in off-line channels, σ_{τ} (see Table 2), which includes contributions from both $\sigma_{on}(v)$ and σ_{BP} . We then scale σ_{τ} by $((T_B(v) + T_{sys})/T_{sys})$ to calculate $\sigma_{on}(v)$. The antenna used to produce the LAB survey is of similar size to an individual VLA antenna, so we use H_I emission from the LAB survey to estimate the brightness temperature as a function of frequency for each source $(T_{\rm B}(v))$, and we assume that the system temperature of the VLA in the absence of H_I emission is $T_{\rm sys} \sim 25$ K. Finally, we calculate the noise spectrum by $\sigma_{\rm r}(v)^2 = \sigma_{\rm on}(v)^2 + \sigma_{\rm BP}^2$ (also see discussion by Roy et al. 2013a). Examples of these noise spectra are displayed as dotted lines above and below the residuals of the Gaussian fits in Figures 2–4. We use the noise spectra to visually inspect the fit residuals, not to quantify the goodness of fit.

3.3. Component Selection: Absorption

The process of Gaussian fitting has many inherent uncertainties, including the determination of number of fit components. The noise level in the fit residuals can be used as a goodness-of-fit indicator, but it cannot easily distinguish between different numbers of components, because adding more components will always reduce the residual noise level without necessarily bringing the fit any closer to an accurate depiction of reality.

To determine the best-fit number of Gaussian components to the absorption spectra, we begin by using a reduced chi-squared $(\chi^2_{\rm red})$ test. We calculate $\chi^2_{\rm red}$ using

$$\chi_{\text{red}}^2 = \frac{1}{\nu} \sum \frac{(O(\nu) - M(\nu))^2}{\sigma_{\tau}^2},$$
 (5)

where O(v) are the observed data, M(v) are the fitted model data, σ_{τ} is off-line rms noise in the absorption spectrum (from Table 2), and ν is the number of degrees of freedom (dof: equal to number of measurements (256 spectral channels) minus the number of fitted parameters, which includes the height, width, and center of each Gaussian function and a constant continuum offset).

For each profile, we would like to include the minimum number of components that brings $\chi^2_{\rm red}$ near to 1.0. However, in many cases, the difference in $\chi^2_{\rm red}$ between fits of different numbers of components is too small to confidently determine the best fit. As an example, we present the case of 3C123 in Figure 2. The central component of the absorption spectrum is very strong and is poorly fit by a single Gaussian component. Including an additional broad component at the base of the central component does improve the fit, and including additional narrow lines improves the fit further.

To compare the $\chi^2_{\rm red}$ values of different possible Gaussian fits, such as those shown for 3C123 in Figure 2, we employ an F-test (e.g., Westmoquette et al. 2007; Dawson et al. 2011) using the IDL procedure mpftest.pro. 10 The F-test allows us to quantify the improvement in $\chi^2_{\rm red}$ as a function of added dof to the Gaussian model. First, the procedure computes the F-value, which is defined as a ratio of $\chi^2_{\rm red}$ and ν values for two models:

$$F = \frac{\chi_{\text{red},1}^2 / \nu_1}{\chi_{\text{red},2}^2 / \nu_2},$$
 (6)

where the subscript "1" denotes the base model that involves the fewest number of Gaussian components, and "2" denotes a model including an additional component (i.e., three additional dof). The probability density function $p_f(f; \nu_1, \nu_2)$ for all F-values (f) described by dof ν_1 and ν_2

¹⁰ http://purl.com/net/mpfit

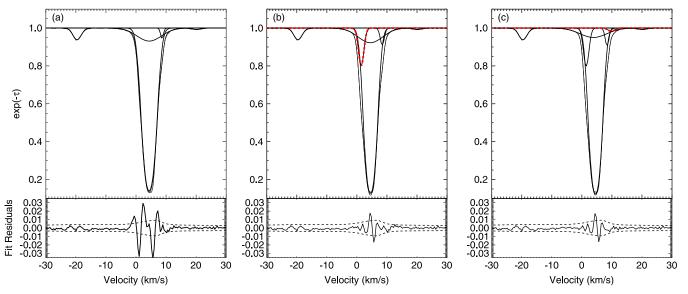


Figure 2. Three Gaussian fits to the optical depth profile in the direction of 3C123 demonstrating the fit improvement with additional components. Top panels: absorption spectrum $(\exp(-\tau))$ with Gaussian components overlaid; bottom panels: fit residuals with $\pm \sigma_r(\nu)$ overlaid (see Section 3.2). (a) Base fit, five components; (b) additional component added (thick red dashed), six total, improving the fit with 99% confidence by the *F*-test, so the component is retained; (c) additional component added (thick red dashed), seven total, improving the fit with 61% confidence by the *F*-test, so the additional component is rejected.

is given by 11

$$p_{f}(f; \nu_{1}, \nu_{2}) = \frac{\Gamma[(\nu_{1} + \nu_{2}/2)]}{\Gamma(\nu_{1}/2)\Gamma(\nu_{2}/2)} \left(\frac{\nu_{1}}{\nu_{2}}\right)^{\nu_{1}/2} \times \frac{f^{1/2}(\nu_{1}-2)}{(1 + f\nu_{1}/\nu_{2})^{1/2}(\nu_{1}+\nu_{2})}.$$
 (7)

From this we calculate the probability that a value f drawn from $p_f(f; \nu_1, \nu_2)$ equals or exceeds the given value of F (Equation (6)), which is given by

$$P_{\rm F}({\rm F}; \nu_1, \nu_2) = \int_{\rm F}^{\infty} df \, p_f(f; \nu_1, \nu_2),$$
 (8)

where $P_{\rm F}$ (or confidence level $C_{\rm F}=1-P_{\rm F}$) is a measure of the probability that the added component merits inclusion in the model.

For the majority of sources, the inclusion of additional Gaussian components results in $C_{\rm F}>0.99$ before $C_{\rm F}$ drops far below $C_{\rm F}\sim0.9$ and indicates low confidence in the most recent component addition. In three cases (sources 3C111, 3C133, and 3C459), the fit parameters varied strongly with the initial guesses, and we observed that the fits remained stable between the final component additions if we applied a cutoff value of $C_{\rm F}=0.97$. Therefore, to apply a uniform standard to all sources, we use a strict threshold of $C_{\rm F}=0.97$ for including components, noting that in all but three cases, the effective cutoff is $C_{\rm F}>0.99$.

As an example, in the case of 3C123, the confidence level of including one additional component (Figure 2(b)) to the base fit (Figure 2(a)) is $C_F = 0.99$, indicating that the additional component exists with high confidence. The confidence level of including a second additional component (Figure 2(c)) in addition to the new fit (Figure 2(b)) is $C_F = 0.61$, and therefore we reject this additional component.

3.4. Component Selection: Emission

The selection of Gaussian components for the expected emission profiles is more difficult. Taking the absorption line fits as fixed in central velocity, peak optical depth, and line width (FWHM), we simultaneously solve for the Gaussian parameters of additional emission components and the spin temperatures of the absorption components given emission information along the line of sight (Equations (3) and (4)). Considering the effects of stray radiation on the emission profiles and the complexity of the fits, we select a minimum number of components that brings the fit residuals below the $3\sigma_{E_{xp}}$ (ν) level. We then apply a similar F-test as in the absorption component selection and add additional components until the confidence level of the fit improvement drops below the cutoff ($C_F = 0.97$).

Given the final selection of Gaussian components, we then solve the radiative transfer equations again for all possible orderings of the N absorption components along the line of sight. We repeat this line of sight iteration for all permutations of F_k , the fraction of WNM unabsorbed by intervening CNM (see Section 3.1) among the K emission components. If the total number of absorption components was large (defined here as greater than or equal to 6), we only varied the order of the most blended components at the center of the spectrum. The effect of different CNM cloud order on T_s is very small compared with the effect of different values of F_k per emission component; therefore, we held the more isolated components in these complex spectra fixed in their LOS order with little consequence to the derived T_s values for the overall fit.

4. SELECTED EXAMPLES

To illustrate the fitting method further, we select four example sources and display their spectra and Gaussian decompositions in Figure 3. The top panel of each plot contains the emission profile, $T_{\rm exp}$ (ν), from HT03, a2770, or LAB (thin solid), the total fit to $T_{\rm exp}$ (ν) (thick solid), the total absorption contribution to the emission profile, $T_{\rm B,ABS}(\nu)$

¹¹ NIST/SEMATECH e-Handbook of Statistical Methods, http://www.itl.nist.gov/div898/handbook/, 01/2015.

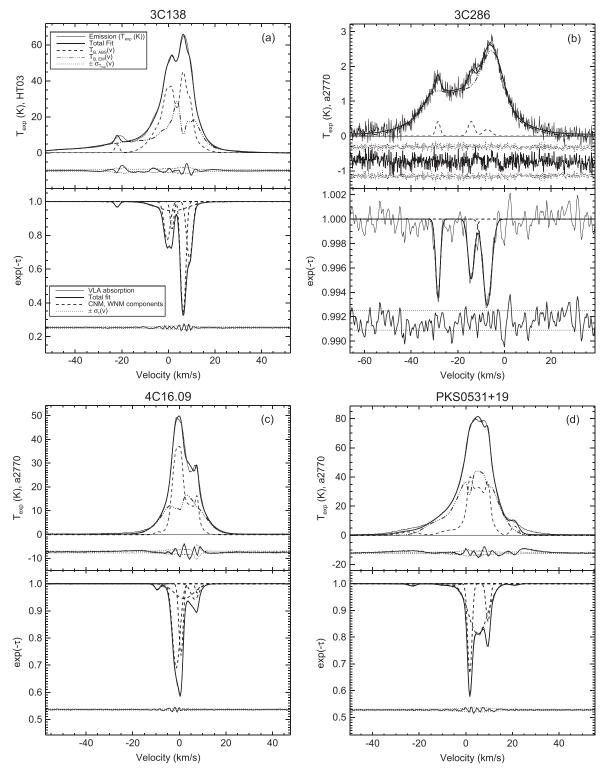


Figure 3. Gaussian fitting decomposition for 4/31 completed sources. The sources are displayed in two-panel plots, where the top panel displays the emission profile (from HT03, a2770, or the LAB survey) and the bottom panel displays the VLA absorption profile. The fits are overlaid in several forms, including total CNM and WNM contribution and individual components, according to the inset legend in panel (a). Residuals in the fits are offset at the bottom of each panel, with $\pm \sigma_{T_{exp}}(\nu)$ (top; see Section 2.4) and $\pm \sigma_r(\nu)$ (bottom; see Section 3.2) to illustrate the goodness of fit.

(Equation (1), dashed), and the total emission-only contribution, $T_{\rm B,EM}(\nu)$ (Equation (1), triple-dot-dashed). The bottom panel of each plot contains the VLA absorption profile (thin solid), total fit to the absorption profile (thick solid), and individual Gaussian components (dashed). The residuals of

each fit are plotted at the bottom of each panel, with noise envelopes $\sigma_{T_{\text{exp}}}(v)$ (Section 2.4) and $\pm \sigma_{\tau}(v)$ (Section 3.2) to illustrate the goodness of fit (dotted).

We compare in detail our Gaussian decomposition with overlapping H_I absorption line surveys, including HT03,

Mohan et al. (2004), and Roy et al. (2013b). All three surveys fit Gaussian functions to their absorption lines and followed different strategies. For example, Roy et al. (2013b) fit increasing numbers of Gaussian functions until χ^2_{red} for the fit was as close to 1 as possible. This resulted in a minimum of 1, maximum of 20, and median of 7 Gaussian components over their 30 spectra. This approach requires detailed knowledge of the spectral noise properties, as well as the assumption that Gaussian functions are the proper representation of all components, which can fail if line broadening is not due to thermal and/or turbulence motions. Our method also makes these assumptions, but we fit fewer components per spectrum (minimum of 1, maximum of 11, and median of 5) to not "over-fit" at the expense of inferior $\chi^2_{\rm red}$ values for the fits. In another approach, HT03 stress that human judgment is necessary for producing reliable Gaussian fits. For example, two fitted components with similar central velocities and FWHMs could in reality be a single component with a non-Gaussian intrinsic line shape. No Gaussian decomposition is a unique solution, and it is impossible to prove which solution is most physically relevant, but the differences between our respective Gaussian fitting strategies will affect the comparison of our results. We emphasize that our F-test method for component selection imposes a uniform standard to a nonunique fitting problem and aims to make our decisions reproducible.

4.1. 3C138 (Figure 3(a))

3C138 is included in the Millennium Arecibo survey (HT03), and they identified many similar, strong components, as we do, in their Gaussian decomposition. As seen in Figure 3(a), in addition to narrow cold components at velocities 9.1, 6.4, 1.6, and $-0.5~{\rm km~s^{-1}}$, we identify a shallow broad underlying component, centered at $1.9\pm0.3~{\rm km~s^{-1}}$ with an FWHM of $15.1\pm0.6~{\rm km~s^{-1}}$. This corresponds to a maximum kinetic temperature of $T_{k,{\rm max}}=5000~{\rm K}$ and, with a fit to the emission profile (from HT03), corresponds to a spin temperature of $456\pm40~{\rm K}$. The maximum spin temperature derived by HT03 for an absorption component in the direction of this source is $T_s=380\pm23~{\rm K}$, corresponding to a similar component at $1.8~{\rm km~s^{-1}}$.

This source is also included in the Roy et al. (2013b) WSRT/GMRT/ATCA survey. Whereas we fit a total of six components before the fit ceases to improve significantly by the *F*-test, Roy et al. (2013b) fit 13 components. Given the complex nature of the spectrum and the large difference in total numbers of components, there are few closely matching components between the two decompositions.

4.2. 3C286 (Figure 3(b))

With a sensitivity of $\sigma_{\tau} = 9 \times 10^{-3}$, HT03 were unable to detect H I absorption in the direction of 3C286. Stanimirović & Heiles (2005) demonstrate that with additional integration times at the Arecibo Observatory, weak absorption lines below the HT03 sensitivity threshold are easily detected, which can have important implications for HT03's measured fractions of H I in the CNM, WNM, and thermally unstable phases. For 3C286, they find three velocity components at -28.8, -14.3, and -7.4 km s⁻¹, with $T_{k,\text{max}} = 106$, 115, and 315 K and $T_s = 89 \pm 7$, 37 ± 4 , and 30 ± 20 K. We find similar velocity components, at -28.5, -14.3, and -7.3 km s⁻¹, with

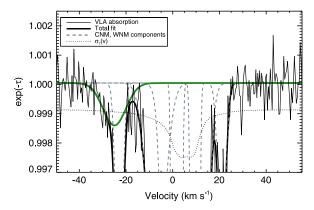


Figure 4. Zoom-in of a broad, warm component (green) in the complex profile toward PKS0531+19. Velocity: $v_{0,\text{LSR}} = -24.96 \pm 4.25 \text{ km s}^{-1}$; FWHM: $\Delta v = 11.5 \pm 9.3 \text{ km s}^{-1}$; peak optical depth: $\tau_{\text{peak}} = 0.15 \pm 0.17$; maximum kinetic temperature: $T_{k,\text{max}} = 2900 \pm 5000 \text{ K}$; spin temperature: $T_s = 1451 \pm 263 \text{ K}$. The dotted line indicates $\sigma_r(v)$.

 $T_{k,\text{max}} = 116$, 220, and 405 K and $T_s = 63 \pm 13$, 84 ± 12 , and 27 ± 9 K. Roy et al. (2013b) find the same three components, in addition to a broad line centered at -8.4 km s⁻¹ with peak optical depth $\tau = 0.001$ and $T_{k,\text{max}} = 5140$ K. Their achieved sensitivity of $\sigma_{\tau} = 3 \times 10^{-4}$ allows them to detect this weak component, whereas our sensitivity of $\sigma_{\tau} = 7 \times 10^{-4}$ puts it below our detection limit. We note that they do not discuss the effect of BP instability on their detection of broad, weak lines.

4.3. 4C16.09 (Figure 3(c))

Although 4C16.09 is not included in the Millennium survey (HT03), it is included in the Mohan et al. (2004) GMRT survey of H_I absorption. They achieve a mean survey sensitivity in optical depth of $\sigma_r \sim 3 \times 10^{-3}$, and the spectra have velocity resolution of 2.1 km s⁻¹ over roughly 350 km s⁻¹. Our absorption profile agrees well in shape with their results. They detect two narrow absorption components, at velocities 7.5 and 0.2 km s⁻¹ with corresponding spin temperatures $T_s = 30$ and 45 K, respectively (Mohan et al. 2004). We detect components at similar velocities, 7.6 and 0.7 km s^{-1} , in addition to four additional absorption components (see Figure 3(c)). We identify two additional, broad emission components that are prominent in the expected emission profile and produce a maximum spin temperature of $T_s = 240 \pm 10$ K. In comparison, Roy et al. (2013b) have the same sensitivity of $\sigma_{\tau} = 8 \times 10^{-4}$ and find eight Gaussian components.

4.4. PKS0531+19 (Figure 3(d))

The profile in the direction of PKS0531+19 is highly complex. Detected by HT03 in the Millennium Survey, they identify four narrow absorption components at velocities 9.6, 5.5, 1.8, and -23.1 km s^{-1} (HT03). We detect features at similar velocities, in addition to two broad, shallow components centered at 21 and -25 km s^{-1} corresponding to spin temperatures of $T_s = 1129 \pm 74 \text{ K}$ and $1451 \pm 263 \text{ K}$. In Figure 4 we zoom in on the second of these components, shown by the thick green line. This source is a good example of the benefit of high sensitivity. The rms noise in the absorption profile is $\sigma_T = 5 \times 10^{-4}$, so that the broad component with peak optical depth equal to $\tau = 0.0015$ is a 3σ detection. HT03

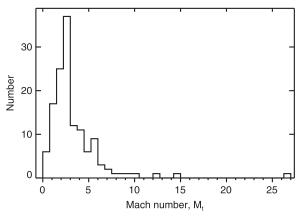


Figure 5. Histogram of turbulent Mach number M_t for all absorption-detected Gaussian components, calculated from Equation (11) (Heiles & Troland 2003b, Equation (17)).

achieve a sensitivity of $\sigma_{\tau} \sim 0.0015$ in their absorption profile toward this source and therefore did not fit a Gaussian function to this line given that it fell below their 1σ level.

5. PROPERTIES OF COLD AND WARM NEUTRAL GAS

Following complete decomposition of all absorption and emission profiles with Gaussian functions, we can use estimates of temperature and column density to infer properties of the CNM and WNM.

5.1. Temperature

The FWHM (Δv) of each Gaussian function determines its maximum kinetic temperature, $T_{k,\max}$, by

$$T_{k,\text{max}} = m_{\text{H}} / (8k_{\text{B}} \ln(2)) \times \Delta v^2 = 21.866 \times \Delta v^2,$$
 (9)

for hydrogen mass $m_{\rm H}$, Boltzmann's constant $k_{\rm B}$, and FWHM $\Delta \nu$ in km s⁻¹ (e.g., HT03). This quantity contains contributions from both thermal broadening and turbulent gas motions so that

$$T_{k,\text{max}} = T_k + \frac{m_{\text{H}} v_{\text{turb}}^2}{2k_{\text{B}}},\tag{10}$$

where T_k is the true kinetic temperature of the gas (e.g., Liszt 2001). Therefore, $T_{k,\text{max}}$ is an upper limit to the kinetic temperature in the presence of turbulent broadening. As shown by Heiles & Troland (2003b), nonthermal motions in the CNM are characterized by a turbulent Mach number (M_t) of $M_t \sim 3$, implying that CNM gas is supersonic. To estimate M_t , we solve Equation (10) for v_{turb}^2 and then assume that this line-of-sight turbulent velocity is $\sqrt{(3)}$ times the three-dimensional turbulent velocity $(v_{\text{turb},3D})$. The turbulent Mach number M_t is given by $v_{\text{turb},3D}^2/C_s^2$, where C_s is the isothermal sound speed. We use C_s because thermal equilibrium is established quickly in the CNM, which dominates the absorption profiles (Heiles & Troland 2003b). Following Heiles & Troland (2003b), we adopt $C_s^2 = kT_s/1.4m_{\text{H}}$ for mean atomic weight $1.4m_{\text{H}}$.

Therefore, the turbulent Mach number is given by

$$M_t^2 = \frac{v_{\text{turb,3D}}^2}{C_s^2} = 4.2 \left(\frac{T_{k,\text{max}}}{T_s} - 1 \right),$$
 (11)

which is Equation (17) from Heiles & Troland (2003b). In Figure 5, we display a histogram of M_t for all 21-SPONGE absorption-detected Gaussian components, which has a peak at $M_t \sim 3$ (median $M_t = 2.86$) and agrees with the results from HT03. The distribution is strongly peaked, and 40% of all components have Mach numbers between 2 and 4.

The spin temperature is determined by the ambient radiation field, collisions between hydrogen atoms, electrons, and protons, and Ly α scattering. For the CNM, high densities allow the collisional contribution to dominate 21 cm excitation so that T_s is expected to be equal to T_k . At low densities, i.e., in more diffuse WNM gas, collisions are not sufficient to thermalize the 21 cm transition and therefore T_s is expected to be less than T_k (e.g., Liszt 2001).

In the case of 12 sources, one or more of the Gaussian functions fit to the absorption spectrum did not have a corresponding spectral feature at the same velocity in emission (likely due to the cold component occupying a very small solid angle; Heiles & Troland 2003a). Therefore, the converged T_s values for these components are unreasonably low, <1 K. Given the uncertain presence of stray radiation in the Arecibo emission profiles, we take a conservative approach for estimating T_s for these components. We adopt the median M_t value measured over all fitted Gaussian functions, $M_t = 2.86$, and solve Equation (11) for T_s and its error given $T_{k,\max}$ and its error

5.2. Column Density

We estimate the H_I column density of the absorbing H_I using the expression

$$N(H I, ABS) = C_0 T_s \int \tau(v) dv, \qquad (12)$$

where $C_0 = 1.823 \times 10^{18} \, \mathrm{cm}^{-2} \, \mathrm{K}^{-1} \, (\mathrm{km \ s}^{-1})^{-1}$, $T_{\rm s}$ is the derived spin temperature, and $\tau(\nu)$ is the optical depth as a function of velocity in $\mathrm{km \ s}^{-1}$. For each $n\mathrm{th}$ absorption component, we use parameters from the Gaussian fit to calculate the column density, so that

N(H I, ABS)_n = 1.064 ×
$$C_0$$
 × $T_{s,n}$ × $\tau_{0,peak,n}$ × Δv_n , (13)

where $(T_{s,n}, \tau_{0,peak,n}, \Delta v_n)$ are the (spin temperature, peak optical depth, and FWHM in km s⁻¹) of the *n*th component and 1.064 converts the product to the area under a Gaussian function with the given height and width. For the emission components not detected in absorption, we estimate the column density as

$$N(H I, EM) = C_0 \int T_B(v) dv,$$
 (14)

where $T_{\rm B}$ is the brightness temperature. Using the Gaussian fit to the emission profile, we estimate the column density associated with each kth non-absorbing component as

$$N(H I, EM)_k = 1.064 \times C_0 \times T_{0,k} \times \Delta v_k,$$
 (15)

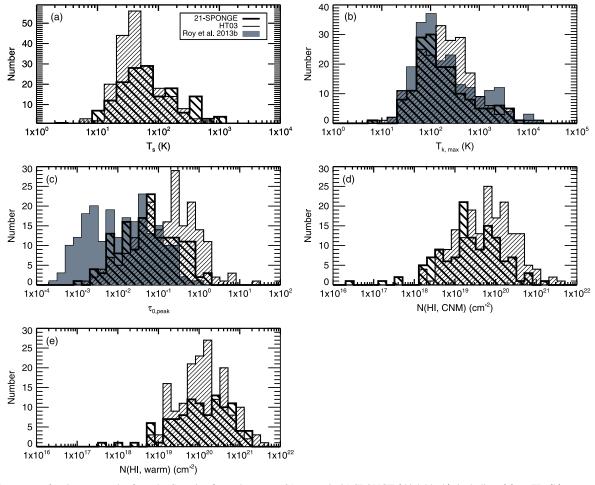


Figure 6. Histograms of various properties from the Gaussian fits to the current 31 sources in 21-SPONGE (thick black), including: (a) T_s (K), (b) $T_{k,max}$ (K), (c) peak optical depth in absorption, $\tau_{0, peak}$, (d) N(H I, CNM): column density of all CNM components, defined as those with $T_s < 200$ K, (d) N(H I, warm): column density of all "warm" components, defined as those with $T_s < 200$ K and those detected only in emission. The results for the Millennium Survey (HT03, thin black) and the WSRT/GMRT/ATCA survey by Roy et al. (2013b) (shaded gray) are included for comparison. Results from Roy et al. (2013b) are not included in panels (a), (d), and (e) because they do not compute these parameters for individual Gaussian components.

where $T_{0,k}$ and Δv_k are the peak and FWHM in km s⁻¹ of the kth component.

6. COMPARISON WITH PREVIOUS SURVEYS

In Figure 6, for all absorption-detected Gaussian functions we display histograms of (a) spin temperature (T_s) , (b) maximum kinetic temperature $(T_{k,\max})$, (c) peak optical depth $(\tau_{0,\text{peak}})$, (d) column density for all CNM clouds, defined as those with $T_s \leq 200$ K, (N(H I, CNM)), and finally (e) column density for all warm clouds, defined as those emission-only components and absorption-detected components with $T_s \geq 200$ K (N(H I, warm)). We overlay the same quantities for the 79 sources from the Millennium survey (HT03) in the panels of Figure 6 for comparison.

The superior sensitivity of 21-SPONGE allows us to detect absorption lines with smaller τ_{peak} and/or higher T_s than in HT03, which explains the poor agreement between the 21-SPONGE and HT03 distributions in Figures 6(a) and (c). We are therefore more sensitive to low-N(H I, CNM), as shown in Figure 6(d) and in Equation (13).

In Figure 6(a), we detect a strong tail of high- T_s components in comparison with HT03. This results in our median $T_s = 77 \text{ K}$, which is higher than their median value of

 $T_s = 48 \text{ K}$. The maximum T_s we detect is $T_s = 1451 \pm 263 \text{ K}$, compared with the maximum value measured by HT03 of $T_s = 656 \text{ K}$, demonstrating that it is possible to directly measure T_s from warm gas with improved sensitivity in H I absorption.

However, although we have the sensitivity to detect H I at higher spin temperatures than 1500 K directly in absorption, we only detect 32/157 Gaussian components above the expected range for the CNM ($T_s = 40 - 200 \text{ K}$ from Wolfire et al. 2003), and only 4/157 above $T_s = 1000 \text{ K}$. This is a surprising result from 21-SPONGE so far, given that HT03 estimate (based on indirect measurements from H I emission only) that 48% of components should be in the thermally unstable range of $500 \le T_s \le 5000 \text{ K}$. Our current estimate for the thermally unstable fraction in this same range — ~20% by number—is more consistent with estimates from colliding flow models (e.g., Audit & Hennebelle 2005).

In Figure 7, we present cumulative distribution functions of the data in Figure 6(a). A K-S test indicates that the two distributions are highly unlikely to be drawn from the same parent population (K-S = 0.23, p = 0.00). The 21-SPONGE distibrution is much shallower at high temperature, indicating again that we are detecting more gas at higher T_s than was done by HT03 using similar analysis methods.

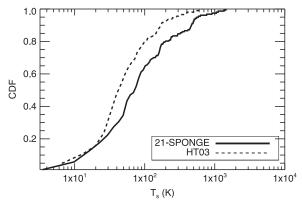


Figure 7. Cumulative distribution function of the T_s values shown in Figure 6(a) for 21-SPONGE and HT03.

In Figures 6(b) and (c) we also include Gaussian decomposition results from the WSRT/GMRT/ATCA survey presented in Roy et al. (2013b) (gray shaded histograms; see Table 1 for survey information). Our two surveys have similar sensitivity in absorption. Following Gaussian decomposition of their absorption spectra, Roy et al. (2013b) do not estimate T_s , N (H I, CNM), or N (H I, warm) for their Gaussian components. As discussed in Section 4, Roy et al. (2013b) fit many more components per spectrum than we do, and therefore they detect many more low- τ lines than either we or HT03 do, as seen by the strong low- τ tail in the gray-shaded histogram in Figure 6(c).

We agree well with both Roy et al. (2013b) and HT03 in $T_{k,\text{max}}$, shown in Figure 6(b). From Equation (9), this implies that we are sensitive to similar absorption line widths. We find a median value of $T_{k,\text{max}} = 160 \text{ K}$, compared with HT03's median value of $T_{k,\text{max}} = 220 \text{ K}$ and Roy et al. (2013b)'s value of $T_{k,\text{max}} = 160 \text{ K}$. We find that 5.7% of components have $T_{k,\text{max}} \leq 40 \text{ K}$, which is below the minimum theoretically expected kinetic temperature for the CNM (e.g., Wolfire et al. 2003), compared wth 4.7% by HT03 and 7.0% by Roy et al. (2013a). At the extreme end of the low- $T_{k,\text{max}}$ values, we find one weak component with $T_{k,\text{max}} = 9 \pm 4 \,\text{K}$ in the direction of 3C345. These low-temperature components can be explained by ineffective photoelectric heating from dust and polycyclic aromatic hydrocarbons along those sightlines, which allows for the existence of very cold clouds with $T_{k,\text{max}} \sim 10 \text{ K}$ (Wolfire et al. 1995; Heiles & Troland 2003b; Roy et al. 2013b).

In Figures 6(d) and (e), it is clear that we generally agree with HT03 in measurements of N(H I, CNM) and N(H I, warm). However, our superior sensitivity in optical depth allows us to detect lines with much lower N(H I, CNM). For example, we are able to detect an individual absorption line with N(H I, CNM) = $(3 \pm 1) \times 10^{16} \,\text{cm}^{-2}$, whereas HT03 measure a minimum column density of $2 \times 10^{18} \, \text{cm}^{-2}$ for individual CNM clouds. An important result from the final 21-SPONGE data release will be constraints on the low-N(H I) end of the CNM column density distribution. McKee & Ostriker (1977) predicted a lower limit to CNM column density of N(H I, CNM) $\sim 10^{17} - 10^{18} \, \text{cm}^{-2}$, derived from balancing radiative losses and conductive heating at the interface between the CNM and WNM at various possible temperatures. As discussed by Stanimirović & Heiles (2005), observational constraints on this lower limit (and its prevalence) can distinguish between different formation and evolution histories of these structures, whether by evaporation into the surrounding medium, transient, dynamic formation at shock interfaces, or condensation from turbulent flows.

6.1. Line-of-sight Properties

In Table 3 we compute line-of-sight column-density-related quantities for the current 21-SPONGE sources, where the subscript "20" indicates units of 10^{20} cm⁻². These quantities include (a) the total CNM column density (Σ N(H I, CNM)₂₀), equal to the sum of the column densities of the absorption-detected Gaussian components with $T_s < 200$ K; (b) the total WNM column densities of the absorption-detected Gaussian components with $T_s > 200$ K plus the column densities of all emission-only Gaussian components (which is a combination of both thermally stable WNM and thermally unstable gas); (c) the total H I column density per line of sight (N(H I, total)₂₀= Σ N(H I, CNM)₂₀ + Σ N(H I, warm)₂₀); and (d) the CNM fraction, $f_{\rm CNM}$, defined as

$$f_{\text{CNM}} = \frac{\Sigma \text{N(H I, CNM)}}{\text{N(H I, total)}}.$$
 (16)

To compare our results, we obtained or calculated the same quanitites for the HT03 and Roy et al. (2013b) samples. For HT03, we used their published fit information to calculate all quantities in the same manner as for 21-SPONGE, described above. To calculate $\Sigma N(H I, CNM)_{20}$, Roy et al. (2013b) began by assuming that all absorbing gas is from the CNM with $T_s = 200 \text{ K}$ and solved Equation (12) to produce upper limits to $\Sigma N(H I, CNM)_{20}$ for each line of sight. We estimated $\Sigma N(H I, warm)_{20}$ from their results by subtracting $\Sigma N(H I, CNM)_{20}$ from $N(H I, total)_{20}$, which they calculated using the "isothermal" method (Spitzer 1978; Dickey & Benson 1982; Chengalur et al. 2013).

We generally agree well with the results from HT03 and Roy et al. (2013b). All three studies measure the same range in $\Sigma N(H I, CNM)_{20}$, between ~0.01 and ~10. We find a median $\Sigma N(H I, CNM)_{20} = 1.76$, compared with 1.45 by HT03 and 1.76 by Roy et al. (2013a). From Figure 7, we detect many more components in absorption with $T_s > 200 \text{ K}$, which have high $N(H I, ABS)_n$ according to Equation (13) and which will increase the total $\Sigma N(H I, warm)_{20}$ along the line of sight. We measure a median $\Sigma N(H I, warm)_{20} = 8.83$, which is much higher than HT03's median value of 3.97 and the Roy et al. (2013a) median value of 1.41. We measure a total column density per LOS $N(H I, total)_{20} = 10.4$ compared with 5.54 by HT03 and 4.33 by Roy et al. (2013a).

Figure 8 displays "box and whisker" plots of $f_{\rm CNM}$ for 21-SPONGE, HT03, and Roy et al. (2013a). By inspection, our results are consistent with the $f_{\rm CNM}$ distribution found by HT03 and Roy et al. (2013a). HT03 do not detect H I absorption in the direction of 15/79 sources, resulting in many values of $f_{\rm CNM}=0$. Whereas we only have one non-detection, we find 9/31 sources with $f_{\rm CNM}\leqslant 0.1$. We measure median $f_{\rm CNM}=0.20$ compared with 0.23 by HT03. We appear to find lower $f_{\rm CNM}$ than Roy et al. (2013b). Out of our 31 sources, we find a maximum $f_{\rm CNM}\sim 0.51$, whereas Roy et al. (2013b) find much higher values, all the way up to $f_{\rm CNM}\sim 1$ with

 Table 3

 Line-of-sight Column Density Parameters

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$f_{ m CNM}$	N(H I, total) ₂₀ (10 ²⁰ cm ⁻²)	$\Sigma \text{ N(H I, warm)}_{20}$ (10 ²⁰ cm ⁻²)	Σ N(H I, CNM) ₂₀ (10 ²⁰ cm ⁻²)	Source
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		(10 ²⁰ cm ²)	(10 ⁻³ cm ⁻)	(10 ²⁰ cm ⁻²)	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.12 ± 0.06	1.36 ± 0.09		0.17 ± 0.09	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.05 ± 0.02	1.34 ± 0.09	1.28 ± 0.09	0.06 ± 0.02	3C286
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.15 ± 0.05	2.37 ± 0.11	2.01 ± 0.03	0.36 ± 0.11	4C12.50
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.02 ± 0.08	2.37 ± 0.19	2.32 ± 0.03	0.05 ± 0.19	3C273
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.03 ± 0.15	2.39 ± 0.38	2.33 ± 0.09	0.06 ± 0.37	3C298
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.05 ± 0.01	4.55 ± 0.13	4.31 ± 0.11	0.24 ± 0.06	4C04.51
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.07 ± 0.08	2.60 ± 0.23	2.43 ± 0.11	0.17 ± 0.20	3C237
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.28 ± 0.07	4.24 ± 0.30	3.05 ± 0.06	1.19 ± 0.30	3C225A
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.22 ± 0.04	4.55 ± 0.21	3.57 ± 0.11	0.98 ± 0.18	3C225B
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.00 ± 0.00	1.01 ± 0.13	1.01 ± 0.13	0.00 ± 0.00	3C345 ^a
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.20 ± 0.14	8.72 ± 1.18	6.96 ± 0.11	1.76 ± 1.17	3C327.1
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.36 ± 0.09	20.59 ± 1.95	13.15 ± 0.78	7.44 ± 1.79	3C147
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.10 ± 0.19	15.76 ± 3.04	14.22 ± 0.48	1.54 ± 3.00	4C33.48
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.21 ± 0.33	45.94 ± 14.94	36.19 ± 0.49	9.75 ± 14.94	3C154
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.51 ± 0.13	59.69 ± 6.69	29.29 ± 0.81	30.39 ± 6.64	3C410
$\begin{array}{llllllllllllllllllllllllllllllllllll$	0.09 ± 0.06	33.86 ± 2.42	30.86 ± 1.33	3.00 ± 2.02	B2050
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.17 ± 0.11	31.69 ± 3.53	26.36 ± 0.55	5.33 ± 3.49	3C409
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.29 ± 0.35	28.84 ± 9.72	20.45 ± 1.48	8.39 ± 9.61	PKS0531
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.11 ± 0.10	36.43 ± 4.42	32.44 ± 2.29	3.99 ± 3.78	3C111
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.27 ± 0.12	35.98 ± 4.05	26.22 ± 0.46	9.76 ± 4.02	3C133
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.23 ± 0.11	26.43 ± 2.89	20.42 ± 0.58	6.01 ± 2.83	3C138
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.21 ± 0.18	24.55 ± 4.80	19.41 ± 1.90	5.15 ± 4.41	3C123
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.11 ± 0.20	10.38 ± 2.10	9.23 ± 0.13	1.15 ± 2.09	3C433
4C16.09 3.27 ± 1.10 8.83 ± 0.24 12.10 ± 1.13 3C454.3 1.99 ± 15.74 5.92 ± 0.63 7.90 ± 15.75	0.49 ± 0.11	22.22 ± 2.26	11.36 ± 0.26	10.86 ± 2.24	3C120
$3\text{C}454.3$ 1.99 ± 15.74 5.92 ± 0.63 7.90 ± 15.75	0.14 ± 0.07	4.95 ± 0.41	4.25 ± 0.19	0.70 ± 0.36	3C48
	0.27 ± 0.09	12.10 ± 1.13	8.83 ± 0.24	3.27 ± 1.10	4C16.09
10000 10017 550 1041	0.25 ± 2.05	7.90 ± 15.75	5.92 ± 0.63	1.99 ± 15.74	3C454.3
J2232 1.21 \pm 0.37 4.29 \pm 0.17 5.50 \pm 0.41	0.22 ± 0.07	5.50 ± 0.41	4.29 ± 0.17	1.21 ± 0.37	J2232
3.81 ± 1.91 9.93 ± 0.27 13.74 ± 1.93	0.28 ± 0.14	13.74 ± 1.93		3.81 ± 1.91	3C78
$3C459$ 1.17 ± 0.49 5.12 ± 0.04 6.29 ± 0.49	0.19 ± 0.08	6.29 ± 0.49	5.12 ± 0.04	1.17 ± 0.49	3C459

^a N(H I, CNM)₂₀ = $(3 \pm 1) \times 10^{16}$ cm⁻².

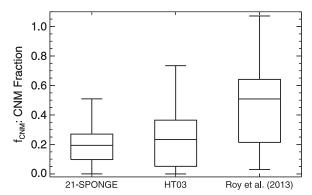


Figure 8. "Box and whisker" plot comparing the CNM fractions (f_{CNM}) for 21-SPONGE with HT03 and Roy et al. (2013a). Each box spans the 25th through 75th percentiles of each distribution, the median value is indicated by the horizontal line within each box, and the bars extend to the minimum and maximum values.

median 0.51. As discussed above, their $\Sigma N(H I, CNM)_{20}$ are strong upper limits, relying on the assumption that all absorbing gas has $T_s = 200 \text{ K}$, which neglects gas along the line of sight at higher and lower temperatures. Therefore, their f_{CNM} values, calculated by dividing the upper limits to $\Sigma N(H I, CNM)_{20}$ by the total isothermal column density (Chengalur et al. 2013), are all strong upper limits.

7. COMPARISON WITH SYNTHETIC OBSERVATIONS

Recently, Kim et al. (2014) used a hydrodynamical simulation of a Milky-Way-like Galactic disk to construct synthetic H I absorption and emission profiles for thousands of sightlines probing the turbulent, multiphase ISM. They calculated "observed" T_s , T_k , N(H I), and $f_{\rm CNM}$ for all lines of sight and found that the majority of sightlines with average LOS spin temperature below 200 K have a CNM fraction between 0.4 and 0.7 (98% have $f_{\rm CNM} < 0.7$; C--G. Kim et al. 2014, private communication). Whereas we measure several CNM fractions within this range, by inspection of Figure 8 and Table 3, we appear to have more measurements below $f_{\rm CNM} = 0.3$ than predicted by the Kim et al. (2014) results. However, in agreement with HT03, Kim et al. (2014) also found many WNM-dominated sightlines with $f_{\rm CNM} = 0$.

Interestingly, Kim et al. (2014) found that synthetically observed line of sight (harmonic mean) T_s values agree within a factor of 1.5 with "true" harmonic mean T_s values computed from the simulation over the full range of integrated optical depth $(10^{-3} < \int \tau dv < 10^2 \, \mathrm{km \ s^{-1}})$. They argue that this implies that there is little overlap between CNM clouds along a line of sight within their $1 \, \mathrm{km \ s^{-1}}$ velocity channels. However, by inspection of our absorption profiles and fits (e.g., Figure 4), it appears that cloud complexes can overlap significantly along every real observed line of sight.

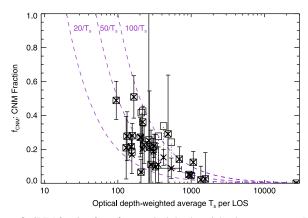


Figure 9. CNM fraction ($f_{\rm CNM}$) vs. optical-depth-weighted average T_s per LOS (Equation (17)). Purple dashed lines indicate the observed trends in CNM fraction with LOS spin temperature from Kim et al. (2014) (their Figures 7(a) and 8(a)). Crosses indicate $f_{\rm CNM}$ calculated from Equation (16) with a cutoff of $T_s = 200~{\rm K}$ to define the CNM; squares indicate $f_{\rm CNM}$ using a cutoff of $T_s = 350~{\rm K}$. Errors in $f_{\rm CNM}$ are shown (solid vertical lines) when they exceed the symbol size. Dotted lines connect crosses and squares when the difference between the two values exceeds the symbol size.

In Figure 9 we plot CNM fraction versus the optical-depth-weighted LOS spin temperature, $T_{s,obs}$. This weighted spin temperature, $T_{s,obs}$, is calculated from Equation (15) of Kim et al. (2014), which was derived from the "isothermal" column density estimate (Spitzer 1978; Dickey & Benson 1982; Chengalur et al. 2013; Kim et al. 2014) and is given by

$$T_{s,\text{obs}} = \frac{\int \tau(v) \frac{T_{B}(v)}{1 - e^{-\tau(v)}} dv}{\int \tau(v) dv}.$$
 (17)

We display the error in the weighted T_s values when they exceed the symbol size. The squares represent the same quantities with a cutoff for the CNM fraction at $T_s = 350 \text{ K}$ instead of $T_s = 200 \text{ K}$. This increases the value of f_{CNM} in only a few cases, because we only detect 6% of all components in the $200 < T_s < 350 \text{ K}$ regime by number. This shows that our choice of temperature cutoff does not strongly affect the observed trends in f_{CNM} .

Kim et al. (2014) plotted the same quantities (their Figures 7 (a) and 8(a)) and found that $f_{\rm CNM}$, defined by a T_k cutoff at 184 K, varies with $T_{s,{\rm obs}}$ roughly as $f_{\rm CNM} \approx T_c/T_{s,{\rm obs}}$ for $50 < T_c < 100$ K. These $T_c/T_{s,{\rm obs}}$ curves are shown in Figure 9 in dashed purple for $T_c = 20$, 50, and 100 K. Although we see a similar tight trend between CNM fraction and $T_{s,{\rm obs}}$, we find points below the $50/T_{s,{\rm obs}}$ curve, indicating again that we are measuring lower $f_{\rm CNM}$ and motivating us to extend the dashed curves down to $20/T_s$. Kim et al. (2014) possibly produced higher $f_{\rm CNM}$ because they did not include H I-H₂ chemistry and therefore could have overestimated $f_{\rm CNM}$ if some cold, dense H I should have transitioned to H₂ form. This was also noticed by Stanimirović et al. (2014) in an H I emission and absorption line study of the Perseus molecular cloud at the Arecibo Observatory.

Overall, we generally agree with the trend between CNM fraction and optical-depth-weighted LOS T_s ($T_{s,obs}$) produced by the synthetic observations of the Kim et al. (2014) simulation, although our observations increase the scatter in the trend. The agreement is very encouraging considering that our CNM fractions rely on temperature calculation by Gaussian

decomposition, whereas theirs are taken directly from their simulated LOSs. Kim et al. (2014) derived an expression describing this trend based on several assumptions: $T_s = T_k$ in the CNM, the "isothermal" column density equals the true column density (truest for low integrated τ sightlines), and the synthetically observed harmonic mean T_s equals the true harmonic mean T_s (where the agreement is best for $\tau < 0.1$, above which there is scatter of up to 1.5). Finally, in computing $f_{\rm CNM}$, they assume that the CNM fraction is not "extremely small" in order to express the $f_{\rm CNM}$ as a ratio of temperatures instead of column densities (see their Section 3.2, Equation (16), Kim et al. 2014). This last assumption may be the most important to increasing the trend scatter, because we (and HT03) find many sightlines with both small $f_{\rm CNM}$ and small $T_{\rm s,obs}$.

The differences between our results are likely due in part to the fact that Kim et al. (2014) do not include magnetic fields or chemistry to map the transitions between H I and H₂, but the similarities found so far suggest that only small adjustments to the simulations may be necessary to match the observed $f_{\rm CNM}$. We also emphasize that the spatial resolution of a simulation is key for resolving the CNM and appropriately calculating quantities like the CNM fraction (e.g., Audit & Hennebelle 2005). In the future we will apply our Gaussian fitting methods to large volumes of synthetic data from Kim et al. (2014) and other higher spatial resolution numerical simulations using Autonomous Gaussian Decomposition (Lindner et al. 2015). This will be essential to assessing the effect of our analysis techniques on these results and also understanding the biases of the numerical models.

8. COMPARISON OF METHODS FOR ESTIMATING SPIN TEMPERATURE FROM H I ABSORPTION AND EMISSION SPECTRA

Several independent methods are commonly used in the literature to measure T_s from H I absorption and emission observations. The first is the method we use in this work, whereby we estimate a single T_s value for each Gaussian component fitted to both absorption and emission spectra (i.e., solving Equation (1)). This method relies on initial guesses for number of components and their shapes, but it is the only method based on a physical model. As is generally true for the 21 cm line, a Gaussian model is a good representation of the spectral line because the damping wings are insignificant. Although this assumption fails in some cases, shown in this study by the components with $T_{k,\max} > T_s$ (6% have $T_{k,\max} > (T_s + 3\sigma)$), the method is convenient and produces reasonable fits to both simple and complex profiles.

8.1. One Phase per Channel T_s

Assuming that the gas in each velocity channel is at a single temperature (the "one-phase" assumption), dividing the brightness temperature spectrum $(T_{\rm B}(\nu))$ by the absorption profile $(1-e^{-\tau(\nu)})$ produces a spin temperature spectrum, $T_{s,O}(\nu)$, via the following equation:

$$T_{s,O}(v) = \frac{T_{\rm B}(v)}{1 - e^{-\tau(v)}}.$$
 (18)

From this it is possible to measure a single T_s value for every velocity channel. For example, Roy et al. (2013a) use this

method to compute $T_{s,O}$ for each velocity channel above 3σ significance in absorption at 1 km s⁻¹ resolution.

8.2. Line-of-sight Harmonic Mean T_s

Assuming that there is one value of T_s along a full line of sight, the "LOS" harmonic-mean temperature, $T_{s,L}$, from the absorption and emission profiles is given by

$$T_{s,L} = \frac{\int T_{\rm B}(v)dv}{\int \left(1 - e^{-\tau(v)}\right)dv}.$$
 (19)

For example, Kanekar et al. (2011) computed $T_{s,L}$ for the same data from Roy et al. (2013a) to distinguish between CNM- and WNM-dominated lines of sight.

8.3. The Slope Method

It is also possible to measure T_s for individual gas components by estimating the slope or "ridge line" of each linear feature in $T_B(v)$ versus $1 - e^{-\tau(v)}$ space (e.g., Mebold et al. 1997; Dickey et al. 2000). The advantage of this approach compared with Gaussian decomposition is that the solution can be determined directly from the data without fitting iterations or initial guesses. However, this method also requires the assumption that all gas in a given velocity range exists at a single temperature, as is also assumed in the one phase per channel and LOS methods. To improve the slope method parameter estimation, Dickey et al. (2003) developed a two-phase nonlinear least-squares fitting technique to determine the T_s slopes, which we will call the "NLLSQ slope method."

Dickey et al. (2003) carried out a detailed comparison of T_s estimation methods, including Gaussian decomposition and the NLLSQ slope method, and found that in cases of isolated, unblended CNM components, these two methods agree reasonably. In another comparison study, HT03 computed T_s for a sample of their sources using a by-eye version of the slope method and similarly concluded that the two methods agree in the case of unblended CNM components, even if there are blended, weaker WNM components present. Dickey et al. (2003) re-processed all 79 HT03 emission and absorption pairs using the NLLSQ slope method and found a median spin temperature per component of $T_s = 31$ K, which is lower than the median value per fitted Gaussian functions by HT03 of $T_s = 48$ K. This suggests that there may be systematic differences between the two methods.

In the comparisons made by Dickey et al. (2003) and HT03, the T_s values from the NLSSQ slope method tend to be lower than the Gaussian-derived T_s . This is due to the fact that spectral features in H_I emission and absorption profiles do not always have the same shape. If channels in emission corresponding to narrow absorption have similar brightness temperature to channels with no corresponding absorption, the slope of the opacity feature will be small. HT03 note that this is because component emission is determined by the product of both optical depth and T_s , so that broad, warm components dominate emission and narrow, cold components dominate only in absorption. We will conduct a detailed comparison of the Gaussian and NLLSQ T_s derivation methods upon completion of the 21-SPONGE data collection. In addition, we plan to use synthetic spectra from numerical simulations, where the input T_s values are known, to assess and quanitfy their associated biases.

8.4. Applying Methods to 21-SPONGE Data

From a preliminary analysis of five 21-SPONGE sources (3C286, 3C225A, 3C225B, 3C237, and 3C298), we find that the NLLSQ slope method temperatures are mostly in the range $25 < T_s < 100 \text{ K}$, which agrees well with the peak of our T_s distribution (Figure 6(a)). In Figure 10 we compare the Gaussian fit, one-phase-per-channel, and LOS harmonic mean methods by applying them to the 21-SPONGE emission and absorption spectral pairs. For the one-phase-per-channel method, for each source we used Equation (18) and included the T_s values for all channels with absorption signals above the $3\sigma_{\tau(v)}$ level. In Figure 10(a), we plot histograms of T_s for (1) the Gaussian decomposition method (thick green, "G"), (2) the one-phase-per-channel method (thin black, "O"), and (3) the LOS harmonic mean method (shaded gray, "L"). In Figure 10(b) we display cumulative distribution functions for the three T_s methods.

Based on the CDFs of the three T_s distributions in Figure 10(b), the one-phase-per-channel and LOS-integrated methods agree well (K-S = 0.18, p = 0.35). Both methods rely on the assumption that there is a single-phase medium in each measurement interval (either velocity channel or full line of sight), which over-simplifies the reality that the ISM is a complex, multi-phase mixture of gas at many temperatures. The one-phase assumption overestimates T_s , because within each velocity channel (and line of sight) narrow components at lower temperatures can cumulatively produce a stronger absorption or emission signal, thereby biasing the average T_s measurement to high values. As previously discussed by Dickey et al. (2000) and Dickey et al. (2003), the NLLSQ slope and Gaussian methods provide systematically lower values of T_s than the single-phase approximations. This is supported by strong disagreements in Figure 10 (p = 0.00between both G and O, and G and L).

The median values of the Gaussian, one-phase-per-channel and LOS methods are $T_{s,G} = 77 \text{ K}$, $T_{s,O} = 340 \text{ K}$, and $T_{s,L} = 290 \text{ K}$. Wolfire et al. (2003) model the multi-phase ISM with detailed analytical prescriptions for heating and cooling and show that the CNM should have a spin temperature of $40 \le T_s \le 200$ K. The Gaussian fit method best reproduces this predicted range, although the T_s values in Figure 10 also contain components associated with thermally unstable gas in addition to the dominant CNM. Furthermore, Figure 10 shows that the Gaussian fit method is the most successful in reproducing the analytical prediction for the lower limit to CNM T_s . The LOS method in particular misses a large fraction of the CNM T_s distribution, as it predicts that all gas should have $T_s > 200$ K. As discussed by Dickey et al. (2009), the T_s single-phase (i.e., O and L) T_s methods provide estimates of the mean temperature or the mixture of CNM and WNM along the line of sight, rather than physical temperatures of individual structures.

9. SUMMARY

In this paper we present methods, data, and preliminary results from the first half of 21-SPONGE, a large H I absorption survey at the Karl G. Jansky VLA. The absorption data are complemented by emission data from the Arecibo Observatory, whose $\sim\!3'\!.5$ beam at 21 cm provides the best available single-dish complement to the $\sim\!1''$ VLA beam so that we come closer by orders of magnitude than previous

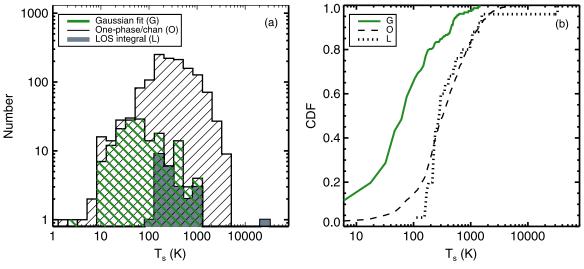


Figure 10. Comparison of temperature derivation methods for the 21-SPONGE survey. (a) Histograms of T_s for Gaussian decomposition of H I absorption and emission lines (thick green), "one-phase" T_s per 0.42 km s⁻¹ channel (thin black, Equation (18)), and integrated T_s per LOS (shaded gray, Equation (19)). (b) Cumulative distribution functions comparing the three temperature distributions from panel (a).

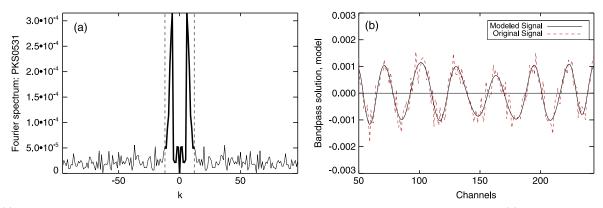


Figure 11. (a) FT spectrum of a bandpass solution, with the boundaries of the applied step-function filter overlaid as dashed lines. (b) Model of the bandpass solution (solid black), computed as the inverse FT of the filter-convolved FT spectrum of the bandpass solution. The bandpass solution is overlaid as the dashed red line.

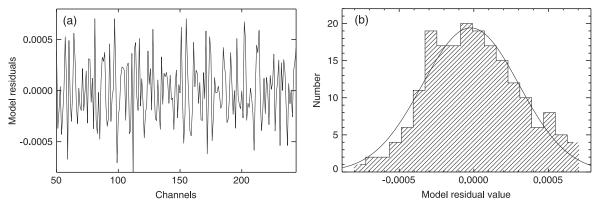


Figure 12. (a) Residuals of the FT model to the bandpass solution displayed in Figure 11 (i.e., bandpass solution minus model). (b) Histogram of the residuals to check if they are well represented by a Gaussian distribution, as would be expected in the case of a successful model. A Gaussian model is overlaid (solid black line) to illustrate this.

studies to sampling the same gas populations in absorption and emission. By obtaining extremely high sensitivity VLA H_I absorption lines, we detect signatures of both cold and warm ISM directly in absorption and, in combination with emission, directly determine the temperatures and column

densities of individual components along the line of sight. We describe the observation and data reduction strategies and discuss details of line fitting and parameter estimation in this paper. Important initial results from the first half of the survey include:

Table 4
Bandpass Solution Parameters

Information:			Fit Parameters:			
Target Name	Obs. Date	Array Configure	rms noise ^a	Amplitude ^b	Period ^b	Phase ^c
			(per channel)		(channels)	(channel)
3C120D1	03/11	В	0.00049	0.0014	30.1	120
3C120D2	03/11	В	0.00047	0.0014	29.9	120
3C286	05/11	В	0.00064	0.0016	29.9	122
3C225BD1	05/11	BnA	0.00049	0.0015	30.0	121
3C225BD2	05/11	BnA	0.00049	0.0015	30.3	121
3C225BD3	05/11	BnA	0.00042	0.0013	30.1	120
4C12.50	05/11	BnA	0.00048	0.0014	30.0	120
3C345	06/11	BnA-A	0.00074	0.0017	30.1	120
3C298	06/11	BnA-A	0.00057	0.0015	29.8	121
4C32.44D1	05/11	BnA-A	0.00040	0.0014	29.9	122
4C32.44D2	06/11	BnA-A	0.00063	0.0015	29.9	120
4C32.44D3	06/11	BnA-A	0.00057	0.0015	29.8	122
3C48	08/11	A	0.00048	0.0014	30.0	120
4C16.09	09/11	A	0.00037	0.0014	30.0	120
4C16.09.2	09/11	A	0.00031	0.0013	29.9	120
3C133	09/11	A-D	0.00035	0.0014	30.1	120
PKS0531	09/11	A-D	0.00031	0.0013	29.9	120
3C111	04/12	C	0.00042	0.0014	29.9	120
3C154D1	04/12	С	0.00057	0.0017	30.2	122
3C154D2	04/12	C	0.00033	0.0013	29.9	120
3C123	05/12	CnB	0.00041	0.0015	30.1	120
3C138	05/12	CnB	0.00041	0.0014	29.9	122
3C410	07/12	В	0.00057	0.0016	29.6	123

^a The rms noise calculated in the residuals of the bandpass solution *after* removing the ripple model.

- 1. We achieve median rms noise in optical depth of $\sigma_r \sim 9 \times 10^{-4}$ per 0.42 km s⁻¹ channel over the 31 sightlines probed by 21-SPONGE so far. This allows us to directly probe absorption signals from both cold and warm H I. We are able to achieve this sensitivity in part by maximizing the signal-to-noise ratio in our BP calibration solutions, which we accomplish by characterizing periodic structures within the solutions and combining calibration observations over time.
- 2. Following a careful Gaussian decomposition of all 31 H I absorption detections, we estimate T_s and N(H I) for 157 Gaussian components. We find a maximum spin temperature per individual component of $T_s = 1451 \pm 263$ K, which is more than a factor of 2 higher than the maximum Gaussian component spin temperature measured by the Millennium Arecibo H I Survey (Heiles & Troland 2003; HT03). We are sensitive to lower N(H I, CNM) due to our better sensitivity in optical depth and detect individual clouds with N(H I, CNM) as low as $(3 \pm 1) \times 10^{16}$ cm⁻².
- 3. We compute total CNM column density, total WNM column density, total H I column density, and CNM fraction along each of the 31 emission and absorption sightlines. We detect similar total CNM column densities, defined as the total column density of all Gaussian components per sightline with $T_s \leq 200$ K, as HT03 and Roy et al. (2013a). We find larger values of total "warm gas" column density, defined as the total column density of all absorption-detected Gaussian components with $T_s > 200$ K and the components only detected in

- emission, due to the fact that we are sensitive to warmer gas in absorption than HT03. We find consistent CNM fractions ($f_{\rm CNM}$) with those found by HT03 and Roy et al. (2013a), although the Roy et al. (2013a) values are all upper limits.
- 4. We observe the same trend between CNM fraction and harmonic mean LOS spin temperature found by the synthetic-observation analysis of a hydrodynamic Galaxy simulation by Kim et al. (2014). The agreement in the trend is encouraging given that our calculations rely on Gaussian decomposition to estimate CNM fraction and theirs are taken directly from the simulation, suggesting that the Gaussian decomposition method is successful.
- 5. In a comparison of T_s estimation methods, we find that one-phase or isothermal assumptions overestimate T_s values relative to individual Gaussian fits. The T_s distribution produced by multi-phase fits via Gaussian decomposition better reproduces theoretically expected lower limits for individual CNM clouds based on detailed heating and cooling analytical models.

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^b Calculated using the periodogram analysis of the solution (i.e., these are the parameters of the dominant component).

^c Starting channel of a new period nearest to the center of the solution.

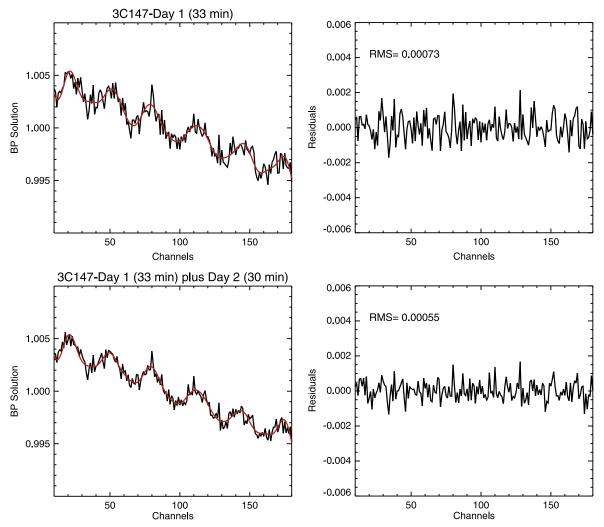


Figure 13. Example of combining bandpass solutions. We fit the bandpass solutions (left) for the presence of a 59 kHz ripple and remove this model (shown in red) to produce the panels on the right, from which we measure the rms noise in the solution. The top panels are from a single observation, and the bottom panels are the results of adding an observation 4 days later.

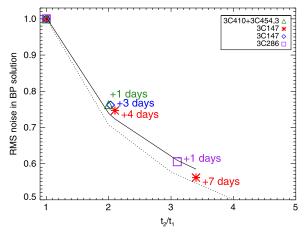


Figure 14. Improvement in rms noise in a bandpass solution (*y*-axis) by combining observations in time, thereby increasing the total integration time (*x*-axis). Symbols denote measurements, and the solid line is a linear fit to the data. The index of the fit is -0.44 ± 0.02 , compared to the theoretical expectation of an index equal to -0.5 (e.g., noise decrease by factor of $1/\sqrt{t_2/t_1}$, shown by the dotted line).

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APPENDIX Bandpass Calibration

A.1 59 kHz Ripple

We find that all BP solutions obtained by 21-SPONGE contain a sinusoidal "ripple" with a period of 59 kHz (or FWHM $\Delta \nu \sim 12\,{\rm km\,s^{-1}}$ at our velocity resolution) and amplitude of ~0.0015. The period, amplitude, and phase of this ripple are constant between array configurations and time of year. After investigating the stability of the ripple, we

determined that it is caused by FIR filters in the WIDAR correlator applied prior to correlation, which are used to shape the BP. The constant relative amplitude, phase, and period of the ripple can all be explained in this context.

To estimate the quantitative properties of the ripple, we first fit and remove the linear BP slope and zoom in on the central channels of the BP solution (channels 50–200 out of a total 256, shown in Figure 11(b)). The linear slope does not affect our ability to detect wide absorption lines, and we are only interested in determining the parameters of the ripple and correcting for it.

We then compute the Fourier transform (FT) spectrum of this flattened, zoomed solution (see Figure 11(a)). Next, we multiply this FT spectrum with a simple step function filter to isolate the dominant periodic components. The boundaries of the filter are shown in Figure 11(a) as vertical dashed lines. We then compute the inverse FT of the filter-multiplied FT spectrum (i.e., the thick black line in Figure 11(a)) to model the periodic component. The modeled signal is displayed by the solid black line in Figure 11(b), along with the original slope-subtracted BP solution (dashed red line).

As a test of the success of the model, we compute the residuals by subtracting the model from the BP solution (see Figure 12(a)). We then compute a histogram of these residuals to observe if they are well represented by a Gaussian distribution, which we expect if the model is reasonable (see Figure 12(b)). In this example, a K-S test between the residuals and a Gaussian distribution returns p = 0.55, indicating that the noise is consistent with being drawn from a Gaussian distribution. From this, we can conclude that the model does a reasonably good job of isolating the dominant periodic components of the BP solution. We compute the rms noise in these residuals as an indicator of the noise level in the BP solution that is not due to the periodic components. We record various parameters associated with the ripple fit in Table 4 for all BP solutions that we tested, including rms noise in the model residuals, ripple amplitude, period, and phase. The amplitude, period, and phase of the ripple for each observation were calculated using a periodogram, following the methods of Horne & Baliunas (1986).

To test if the presence of the ripple is a function of particular antennas, we separated the BP solutions into three groups of about nine antennas (i.e., antennas 1–9, 10–18, 19–28). After fitting the solutions from these antenna subsets, we find that the ripple exists at a similar power to that in the full solution in all cases. Therefore, we conclude that the effect is not antenna based.

A.2 Time Averaging

To minimize noise levels in BP solutions, we combine BP observations acquired at different times. To compare noise levels in the BP solutions from the original observation and the combined observations, we first model and remove the $59 \, \text{kHz}$ ripple present in all solutions. Figure 13 shows an example of the modeling process. A zoom-in onto a BP solution from one observation of 3C147 (33 minutes of integration) is shown in the top left panel, with the ripple model overlaid in red. The top right panel displays the residuals following the removal of the ripple model, from which the noise in the BP solution is computed. The bottom panels are the same, after adding an additional observation of $3C147 \, \text{from 4 days later}$ (for a total of $33 + 30 = 63 \, \text{minutes}$ of integration).

We expect the noise in the BP solution to decline according to the factor of increase in integration time given by the ideal radiometer equation, or by $1/\sqrt{t_2/t_1}$. For example, for an increase in integration time of $t_2/t_1 = 63/33 = 1.9$, we expect an improvement in noise by a factor of $1/\sqrt{t_2/t_1} = 0.72$. The improvement in noise is 0.00055/0.00073 = 0.75.

In Figure 14 we show the rms noise in the BP solution (computed after removing the ripple) as a function of t_2/t_1 for several different observations (symbols). The solid line displays a fit to the data points, which is linear in log space with a slope of -0.44 ± 0.02 . This is nearly equal to the theoretically expected fit index of -0.5 (e.g., a noise decrease by factor of $1/\sqrt{t_2/t_1}$). This result is highly encouraging, as it demonstrates that VLA BP solutions at this resolution from different days are stable enough to be combined to increase the sensitivity of observations while significantly saving observing time, which is especially useful for very deep observations.

In this process, we are able to combine observations of different sources. In Figure 14, the green triangles are from a trial combining observations of the sources 3C410 ($S_{1.4\,\mathrm{GHz}}=10\,\mathrm{Jy}$) and 3C454.3 ($S_{1.4\,\mathrm{GHz}}=11\,\mathrm{Jy}$) as BP calibrators. The other three cases are combinations of observations of the same BP calibrators, 3C147 ($S_{1.4\,\mathrm{GHz}}=23\,\mathrm{Jy}$) and 3C286 ($S_{1.4\,\mathrm{GHz}}=15\,\mathrm{Jy}$) between several days. These examples represent a common trend in our results.

In later observations, we experimented with including additional 0.5 MHz subbands spaced ± 1.5 , 3 and 4.5 MHz from the H I line. We found that combining these subbands does not significantly improve the noise in the BP solution.

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