# Unsteady Flow and Transition Phenomena in an Axial Flow Compressor

by

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Alan D. Henderson

## Abstract

The unsteady mid-span aerodynamics of an outlet stator row in a 1.5-stage low-speed axial compressor is investigated experimentally and numerically. Two stator blade rows with characteristically different blade profiles are studied: one of standard British C4 section and a controlled diffusion (CD) blade with a circular arc leading edge profile.

A turbulence grid placed at compressor inlet is used to generate turbulence characteristics similar to those occurring in an embedded stage in a multi-stage axial compressor. The stator inlet flow is studied using hot-wire anemometry and compared with previous measurements made in the natural low inlet turbulence configuration of the research compressor. Increased turbulence level enhances the dispersion of inlet guide vane (IGV) wakes. This modifies the interaction between IGV and rotor blade wakes, leading to a more circumferentially uniform flow field at entry to the stator with significantly lower periodic unsteadiness.

Laminar-turbulent transition on a C4 stator blade is studied using an array of surface-mounted hot-film sensors. Comparisons with measurements made at low inlet turbulence show that the increased inlet turbulence level reduces the extent of periodic transitional flow on the stator blade surface. The blade element behaviour flow behaviour at high inlet turbulence closely resembles the low inlet turbulence case with the stator immersed in IGV wake turbulence.

The circular arc leading edge profile of the CD stator produces rapid acceleration and deceleration at the stator leading edge. The influence of this velocity spike on the stator boundary layer development and transitional flow behaviour is studied using an array of surface mounted hot-film sensors. A region of favourable pressure gradient on the suction surface following the leading edge spike has a stabilising effect on the boundary layer, with a large region of flow in a laminar or transitional state. Turbulent spots and instability phenomena in this region are examined for convection speed,

Abstract

growth rate and evidence of relaminarisation. In contrast, the flow on the pressure surface becomes turbulent near the leading edge. The study shows that compressor blade leading edge profiles have a major influence on boundary layer development over the whole surface.

The effect of upstream rotor wake passing on the stability of stator blade boundary layers is examined. The unsteady quasi-three dimensional flow solver, UNSFLO, is used to interpret surface hot-film data and unsteady laminar flow behaviour at the leading edge of both C4 and CD stators. Rotor wake chopping is found to stabilise the pressure surface boundary layer and destabilise the suction surface boundary layer. Examination of hot-film data points to the leading edge as the principal receptivity site for transitional flow phenomena occurring on the suction surface of both the C4 and CD blading.

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## Nomenclature

#### General Variables

Tu

```
c
             blade chord
             skin friction coefficient = 2\tau_w/\rho U^2
c_f
             surface pressure coefficient = (P_1 - p)/(P_1 - p_1)
C_p
D
             diameter
E
             anemometer bridge voltage
             an
emometer bridge voltage at zero flow = ((E^2 - E_o^2)/E_o^2)^3
E_o
H
             boundary layer or wake shape factor = \delta^*/\theta
             blade incidence angle = \alpha - \beta
i
             acceleration parameter = (\nu/U^2)dU/dx
K
L
             length
             static pressure
p
P
             total pressure
R
             radius
             compressor inlet Reynolds number = V_a.c/\nu
Re_a
Re_c
             compressor reference Reynolds number = U_{mb}.c/\nu
             stator inlet Reynolds number = V_1.c/\nu
Re_1
             surface length
s
             dimensionless surface length = s/s_{max}
s^*
             surface length from leading to trailing edge
s_{max}
S
             blade pitch
S^*
             dimensionless pitchwise distance = w/S
             time
t^*
             dimensionless time = t/T
T
             rotor passing period
```

random disturbance level or 'turbulence'

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 $\tilde{T}u$ periodic disturbance level  $Tu_D$ apparent or 'total' disturbance level Ulocal free-stream velocity  $U_{mb}$ mid-blade rotor blade speed  $V_a$ axial velocity at compressor inlet periperal distance waxial coordinate  $\boldsymbol{x}$ flow angle relative to axial direction, turbulent spot spreading angle  $\alpha$ blade angle relative to axial axial direction  $\beta$ turbulent intermittency pressure gradient parameter =  $(\theta^2/\nu)dU/dx$  $\lambda_{\theta}$ integral or 'macro' turbulence scale Λ air density  $\rho$ flow coefficient =  $V_a/U_{mb}$  $\phi$ blade row solidity = c/Skinematic viscosity =  $\mu/\rho$ absolute viscosity  $\mu$ wall shear stress  $\tau_w$ quasi wall shear stress  $au_q$  $\theta$ boundary layer momentum thickness, wake momentum thickness, blade camber angle =  $\beta_1 - \beta_2$  $\delta^*$ boundary layer displacement thickness, wake displacement thickness ξ blade stagger angle total pressure loss coefficient =  $(P_1 - P_2)/(P_1 - p_1)$  $\omega$ 

## **Subscripts**

1	stator blade row inlet
2	stator blade row outlet
cr	critical
in	compressor inlet (upstream from IGV)
le	leading edge
mb	mid-blade
te	trailing edge

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## Acronyms

AVDR axial velocity – density ratio

CD controlled diffusion

CFD computational fluid dynamics

DNS direct numerical simulation

HP high-pressureLAG long axial gap

LDA laser-doppler anemometry

LDV laser-doppler velocimetry

LES large eddy simulation

LP low-pressure

OD outer diameter

PDF probability density function

PVC peak-valley counting

RANS Reynolds-averaged Navier–Stokes

SAG short axial gap

UTAS University of Tasmania

### **Mathematical Notation**

(	)	time	average
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